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RESEARCH MEMORANDUM

SOME CONTROL CONSIDERATIONS FOR RAM-JET ENGINES

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SOME CONTROL CONSIDERATIONS FOR RAM-JET ENGINES

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SUMMARY

Control requirements and parameters were determined from calculated engine performance maps for a fixed-geometry ram jet of a configuration suitable for strategic supersonic missile propulsion. Several control schemes for attaining desired engine performance and for stabilizing missile flight velocity during cruise are presented.

For engine operation at minimum specific fuel consumption, critical diffuser flow conditions must be maintained. This mode of engine operation may be attained by regulation of diffuser exit Mach number with flight Mach number according to a predetermined schedule through a closed-loop fuel control or by the use of an "optimalizing" control that maintains maximum diffuser pressure ratio irrespective of flight Mach number.

Regulation of missile cruise velocity may be obtained by use of a thrust control system in which the engine fuel flow is varied as a function of flight Mach number or by means of an aerodynamic control system, sensitive to flight Mach number, which causes the missile either to dive or to climb in order to increase or to reduce velocity, respectively. The nature of missile response under such control action is presented.

INTRODUCTION

The ram-jet engine offers great potentialities as a propulsion system for supersonic guided missiles because of its simplicity of construction, low specific weight, and economy of operation. The realization of the potential of this power plant is highly dependent upon the development of engine control systems capable of maintaining proper engine operation.

A propulsion system control is, in general, required to perform two basic services; these are (1) to maintain desired engine performance throughout a flight plan, and (2) to minimize departures from desired performance during transients resulting from external disturbances acting on the engine-aircraft system. This second element, which exists for all engine-aircraft systems, assumes greater importance for the supersonic ram jet because engine performance is greatly affected by flight velocity.

In order to analyze the control requirements for a supersonic ram-jet engine, an investigation was made at the NACA Lewis laboratory of the performance of a fixed-geometry ram-jet engine of a configuration considered representative of those desirable for the propulsion of strategic guided missiles. From the computed performance maps thus obtained it was possible to select engine variables suitable for use as control parameters for obtaining certain modes of engine operation. Several control schemes utilizing the selected variables are presented and the advantages and disadvantages of the different schemes are discussed. The second phase of the study is concerned with the interrelation of the ram-jet propulsion system and the aircraft it propels and is concerned with the stabilization of the flight velocity of the engine-missile system. Two methods of stabilizing flight velocity are proposed and the character of the system response to external disturbances is presented. For both elements of this investigation, the principles of operation of these controls, rather than detailed design considerations, are discussed.

METHOD OF ANALYSIS

Engine configuration. - The ram-jet configuration selected for this study is shown schematically in figure 1. This configuration was designed to cruise at a flight Mach number of 3.0 and incorporates a spike-type diffuser. At the design point the ratio of diffuser capture area to combustion chamber entrance area A_0/A_2 is 0.786, which yields a combustion chamber entrance Mach number of 0.199 at design flight Mach number and an engine total temperature ratio of 2.2. (The symbols used herein are defined in the appendix.) The exhaust nozzle is of the convergent-divergent type with a contraction ratio A_5/A_4 of 0.556 and expands to combustion chamber diameter at the exit. The ratio of engine length to combustion chamber diameter is 6.0. The moderate value of the engine temperature ratio at the design condition is in accordance with the requirements of high engine efficiency for strategic missile applications.

Assumptions and method of computation. - The diffuser pressure recovery characteristic assumed for the performance calculations is shown in figure 2, where maximum diffuser pressure recovery is plotted

as a function of flight Mach number for a fixed diffuser geometry designed for a flight Mach number of 3.0. The recoveries indicated compare favorably with those achieved by fixed-geometry single cone diffusers in this Mach number region.

At a given flight Mach number and altitude, specifying the engine temperature ratio defines the internal performance of the engine. One-dimensional flow relations were used in computing the internal performance of the engine. The pressure drop across the flame holders was assumed equal to two combustion chamber entrance velocity heads. For subcritical engine operation, that is, for the diffuser operating at less than the maximum mass flow ratio, it was assumed, for simplicity, that the diffuser pressure recovery was constant at the maximum attainable at the given flight Mach number. For each value of temperature ratio the net thrust, diffuser pressure ratio P_2/p_0, diffuser exit Mach number M_2, fuel flow W_f, and fuel-air ratio were determined. Effective values of fuel flow are used throughout rather than absolute values, which are a function of combustion efficiency. The effective fuel flow is defined as the product of actual fuel flow and combustion efficiency. The fuel characteristics assumed are those of a typical hydrocarbon fuel.

The external characteristics of the engine considered were the additive drag, friction drag, and cowl pressure drag. The additive drag was computed according to the method presented in reference 1. The friction drag was computed using the flat-plate formula of reference 2, which assumes the temperature of the boundary-layer air to be the arithmetic mean of the wall and the free-stream temperatures, and was increased by 5 percent to account for the effect of body geometry on friction drag coefficient. The diffuser cowl was assumed to have a lip angle of 6° and an external length of approximately 0.6 combustion chamber diameters. Cowl pressure drags were estimated from two-dimensional and conical flow considerations. The sum of these drags was subtracted from the net internal thrust to yield what is designated the propulsive thrust F_p of the engine. From the propulsive thrust and the engine effective fuel flow, the specific fuel consumption of the engine was computed.

Engine performance was computed for Mach numbers from 2.6 to 3.4 for altitudes above 35,000 feet. Again, the range of conditions selected for the computations is in accord with conditions considered desirable for long range ram-jet powered missiles.

RESULTS AND DISCUSSION

Engine Performance

The calculation of engine performance indicated in the preceding section provides sufficient data for the preparation of the performance charts shown in figure 3, where engine propulsive thrust is shown as a function of corrected effective fuel flow, engine total temperature ratio, diffuser pressure ratio, and diffuser exit Mach number for a range of flight Mach numbers. Both propulsive thrust and effective fuel flow have been corrected by combustion chamber area to make the charts applicable to any size engine of this configuration and by ambient static pressure to generalize the variables for the effect of altitude pressure in the isothermal region of the atmosphere. Reynolds number effects are neglected in such a generalization.

At any flight Mach number the thrust curves show certain basic characteristics. As effective fuel flow or temperature ratio is increased, thrust increases rapidly as does the diffuser pressure ratio. At the critical point, maximum mass flow through the engine and maximum pressure ratio are attained, and at this point a discontinuity occurs in the slope of the thrust curve. Beyond this point the propulsive thrust increases only slightly with increasing engine temperature ratio or fuel flow; such engine operation is termed subcritical and may be accompanied by a diffuser flow instability termed "pulsing" or "buzz" (reference 3).

The variation of thrust specific fuel consumption with effective fuel flow and thrust is shown in figure 4 for several flight Mach numbers. It can be seen that minimum specific fuel consumption occurs at the point of critical diffuser flow (fig. 3) and that the increase of propulsive thrust obtained by operating in the subcritical region is accompanied by large increases in thrust specific fuel consumption. Supercritical operation, that is, operation at reduced pressure recoveries and thrust, also yields increased values of specific fuel consumption, but there is a region near the critical point where only a slight reduction in engine efficiency occurs.

In order to achieve a specified range with minimum missile weight it is desirable to operate a ram jet at its point of minimum specific fuel consumption, for at this point not only maximum engine efficiency but also almost maximum thrust is attained at a given flight Mach number. As indicated by the preceding performance curves, this condition of minimum specific fuel consumption occurs at the critical diffuser condition and thus establishes a possible control requirement for long range missile configurations; that is, the control must maintain critical diffuser flow.

Control Relations

It can be seen that the basic control considerations for the ram-jet engine operating at supersonic flight speeds are inherently concerned with the characteristics of the inlet diffuser. In effect, the control problem for the ram jet may be resolved into the determination of the method of manipulation of the input variable to attain satisfactory diffuser and hence engine performance.

The fixed-geometry ram jet has but one input variable which can be manipulated to obtain the desired engine operation - this variable is engine fuel flow. The effective fuel flow required for critical engine operation is shown in figure 5 as a function of flight Mach number. The fuel flow for this mode of engine operation (minimum specific fuel consumption) increases exponentially with flight speed and varies threefold over the range of Mach numbers shown. In order to maintain critical operation of the engine, it is, of course, possible to schedule the corrected fuel flow as a function of flight Mach number; but this requires accurate knowledge of the variation of combustion efficiency during a flight plan and such a control scheme can offer no positive assurance of proper engine operation.

It is advantageous to utilize some engine variable which is truly indicative of the engine operating point to control the fuel flow to the engine. Two engine parameters which satisfy this requirement and are not functions of combustion efficiency are the ratio of diffuser exit total pressure to ambient static pressure (diffuser pressure ratio) and the diffuser exit Mach number. The variation of these parameters with flight Mach number required for critical engine operation may be obtained from figures 3(c) and 3(d), respectively, and are shown in figure 6. These curves represent, in fact, possible control relations for critical ram-jet operation which can be maintained by variation of engine fuel flow; that is, the desired value of either of these parameters can be used as a scheduled function of the flight Mach number attainable by manipulation of the fuel flow in a closed-loop fuel control. The application of each of these variables in such a control system is now considered.

Control of diffuser pressure ratio. - A block diagram of a possible control system utilizing the control relation between diffuser pressure ratio and flight Mach number is shown in figure 7. In the system shown, flight Mach number is measured by a Machmeter or similar instrument and this signal is fed into a scheduler. This scheduler has built into it a computing device (such as cams or specially wound potentiometers) such that its output bears the functional relation to flight Mach number indicated in figure 6(b). The output of the scheduler is therefore the required value of diffuser pressure ratio. The value of

pressure ratio existing at the diffuser exit is measured and this sig-
nal is fed back to be compared with the required value of P_2/p_0 in an
error detector. Any error or difference between the required and exist-
ing value of pressure ratio acts through a fuel control to vary the fuel
flow in such a manner as to bring the error to zero, thus attaining the
desired operating point. This system is advantageous because it auto-
matically corrects for the variation in ambient pressure with altitude
and is not influenced by variations in combustion efficiency.

This system has, however, one important disadvantage: such a control
may easily be "fooled" into placing the engine in the subcritical region
with attendant loss of efficiency and possible diffuser pulsing. The
manner in which this occurs can be deduced from figure 8, which presents
plots of diffuser pressure ratio against effective corrected fuel flow
at various constant flight Mach numbers. The plot has been subdivided
into supercritical and subcritical operating regions. In the super-
critical engine operating region, an increase in fuel flow results in
an increase in pressure ratio; therefore if the control shown in figure 7
senses a diffuser pressure ratio less than the set value, it will act
to increase the fuel flow and thus raise the diffuser pressure ratio,
bringing the engine toward the critical point. At the critical point,
there is a discontinuity in the pressure ratio curve; the nature of
this discontinuity is a function of the diffuser characteristics. In
general, there are two possible behaviors of pressure ratio in the sub-
critical region - the pressure ratio may have a constant value (as was
assumed for the computations), or it may decrease with increasing fuel
flow (as indicated by the dashed lines) with possible attendant pulsing.
In either event it is possible for the control to increase the fuel flow
continuously in an effort to raise the pressure ratio, and either engine
failure or combustion blow-out will occur. In the case of the flat dif-
fuser characteristic, this could be caused by an error in the control
schedule, a calibration error, for example, such that a value of pres-
sure ratio is set that is higher than the value attainable at the given
Mach number. For a diffuser with a decreasing pressure ratio charac-
teristic, any disturbance which acted to place the engine in the sub-
critical region could initiate the continuous increase of fuel flow.
Therefore, this control scheme would be relatively unsatisfactory for
critical engine operation unless some sort of fuel flow limiting device
were incorporated in the system.

Control of diffuser exit Mach number. - The use of diffuser exit
Mach number to control fuel flow overcomes the principal disadvantage
of the system controlled by diffuser pressure ratio. The control sys-
tem using this parameter is essentially the same as that shown in fig-
ure 7 for the pressure ratio system, the difference being that M_2 is
measured and that the output of the schedule is related to the flight
Mach number by the curve shown in figure 6(a). The system operates in
a similar manner; any difference between the required value of diffuser

exit Mach number and the value existing in the engine acts through the
fuel control to reduce the error to zero, thus attaining the desired
operating point. This system possesses all the advantages of the sys-
tem controlling diffuser pressure ratio - it compensates for changes in
ambient pressure and is also unaffected by variations in combustion
efficiency. Furthermore, the relation between diffuser exit Mach num-
ber and fuel flow is continuous, as can be seen from figure 9, and there-
fore continuous increase of fuel flow cannot be caused by inadvertent
subcritical operation. If the engine should get into the subcritical
region, the value of the exit Mach number would be below that required
for critical operation, which would cause the control to decrease the
fuel flow and thus bring the engine back toward its critical point. Of
course, this system could produce subcritical operation if the schedule
were in error and called for a value of diffuser exit Mach number below
that required for critical operation. In this event, the control would
maintain subcritical operation but would not continually increase the
fuel flow. The chief disadvantage of this system would appear to be the
small order of the variation of the controlled parameter, variation of
M_2 from 0.16 to 0.25 being sufficient to cover almost the complete range
of thrust at a given flight Mach number. This would require the develop-
ment of highly accurate sensing devices to measure the diffuser exit
Mach number.

It should be noted that the control systems just proposed can be
used to attain modes of engine operation other than critical-point oper-
ation, since at any flight Mach number there exist unique relations
among diffuser pressure ratio, diffuser exit Mach number, and engine
thrust. The attainment of any desired mode of engine operation within
the capabilities of the ram jet requires merely the use of a different
control schedule relation in the systems presented. The discussion has
been limited to critical-point operation because, as previously stated,
this manner of engine operation is desirable for long range missile
application.

Optimizing control. - In order to attain critical operation of the
engine, the controls considered have depended upon a schedule of a con-
trolled variable with flight Mach number and as such are subject to
errors and inaccuracies caused by possible variations in engine charac-
teristics due to manufacturing tolerances and other similarly unavoidable
factors. The ram-jet engine possesses, however, a property that makes
possible the elimination of such sources of error and the fullest utili-
zation of the capabilities of the engine. This property is, paradoxically,
the peaks in the pressure ratio curves which were the source of diffi-
culties in the first control system considered. The coincidence of these
peaks with the point of optimum engine performance makes possible the
utilization of the underlying principles of the "optimalizer" control as
proposed in reference 4. Such a system will seek the point of maximum

diffuser pressure ratio at all times and thus will achieve critical
engine operation.

The principle of operation of this control may be illustrated by
a consideration of figure 10. In this figure is reproduced the vari-
ation of diffuser pressure ratio with fuel flow at a constant flight
Mach number. (The decreasing pressure ratio characteristic is shown
here, for this is the most prevalent behavior of diffusers.) The con-
trol operates in the following manner: A small periodic variation in
fuel flow, superimposed on the mean fuel flow, is sent into the com-
bustion chamber. Changes in the diffuser pressure ratio P_2/p_0 result
from the variation in fuel flow and the pressure ratio variations are
measured and compared with the impressed fuel flow variation. If the
engine is in the supercritical region, then, as can be seen from fig-
ure 10, an increase in fuel flow results in an increase in pressure
ratio; for a sinusoidal fuel flow variation, the variation of the para-
meters with time will appear as shown in the lower left. The fuel flow
and pressure ratio signals are essentially in phase. This in-phase
relation between input and output is detected by a phase sensitive device;
the output of the phase detector causes a fuel control to increase the
average fuel flow and thereby brings the engine toward the critical
point. If the engine is in the subcritical region, an increase in fuel
flow will result in a decrease in pressure ratio. This condition is
illustrated in the lower right of figure 10. In this region, the vari-
ation in pressure ratio is essentially 180° out of phase with the fuel
flow and the phase detector output will cause the fuel control to
decrease the fuel flow and therefore bring the engine back toward the
critical point. The control just described is of the "on-off" type in
that the average fuel flow is either increasing or decreasing and is the
simplest possible type of such an optimizing system. Reference 4 dis-
cusses more refined schemes for attaining desirable optimalizing control
performance. (A control of this nature, that is, an optimalizing system,
is under development and is discussed in reference 5.)

This control seeks peak pressure ratio at all times and thus auto-
matically satisfies the requirement for critical engine operation. It
has all the advantages of the previously discussed systems, that is, it
is independent of altitude and combustion efficiency. Under such control
action, there will, of course, be the continuous variation in thrust
caused by the variation of fuel flow, but this can be kept small as
determined by the minimum input signal size acceptable for control pur-
poses. One important requirement for the successful application of such
a control is the existence of a sufficiently wide band of frequencies,
free from noise and interference effects, on either side of the frequency
of the imposed disturbance. Such a band may be difficult to find in a
ram jet because combustion roughness and diffuser pulsing may produce
noise of large amplitude in the diffuser pressure signal over a very
wide range of frequencies.

Flight Considerations

Thus far only the considerations involved in attaining a desired engine operating point have been discussed. The interrelation of missile flight plan requirements and ram-jet performance will now be discussed. Long range missiles powered by air-consuming power plants are normally designed to cruise on the Breguet flight plan, which requires that the missile maintain constant flight Mach number. The operating map of the ram-jet engine considered in this investigation is shown in figure 11(a), in which is plotted the variation of corrected thrust with flight Mach number at several constant corrected fuel flows. These curves are cross plots of the curves of figure 3(a). The cruise flight Mach number for the system considered is 3.0 and at this point the propulsive thrust must equal the missile drag. A typical missile drag curve at constant angle of attack and essentially constant alti-tude is superimposed on the engine map such that cruise with critical engine operation at Mach number 3.0 is attained. Only one equilibrium point is indicated on this figure, the cruise point at Mach number 3.0. The engine map has been subdivided into subcritical and supercritical operating regions.

It is apparent that for an engine operating at constant corrected fuel flow the configuration is unstable in flight velocity; any exter-nal disturbance acting to decrease missile flight speed would place the system in a region where drag is greater than thrust and continuous deceleration would result. On the other hand, a disturbance acting to increase missile velocity places the system in a region where drag is greater than thrust and the decelerating force which exists in this region has a stabilizing effect, tending to restore the system to cruise velocity. If a control designed to maintain critical engine conditions were in operation, the engine thrust line would be that shown by the dash-dot line. Under this mode of engine operation the system is unstable for either form of external disturbance. Similar instability charac-teristics may be deduced from figure 11(b), which shows engine perform-ance at constant diffuser exit Mach number. This velocity instability represents a control problem of prime importance for the cruise phase of a missile flight plan.

Two means for stabilizing missile velocity are considered: The first is to utilize available aerodynamic and gravitational forces to stabilize flight velocity. If, for example, the missile is below cruise velocity, the angle of attack may be decreased. This change in angle of attack decreases the drag and lift and places the missile in a shallow dive to increase the velocity. The second method is to vary engine thrust through fuel flow to provide a restoring force for the missile. For an engine designed to cruise at critical conditions this normally cannot be done safely, for an increase in fuel flow results in subcriti-cal operation which may be accompanied by diffuser instability. Also,

the available increase of thrust is quite small and excessively long
response times would prevail. It is better, to design the engine for
supercritical operation at the cruise velocity which then safely pro-
vides the necessary latitude of thrust variation to stabilize flight
velocity. This design, however, requires an oversized engine to pro-
pel the missile, which results in an increase in missile weight, because
supercritical engine thrust and efficiency are less than those attain-
able at the critical point.

    In order to determine the nature of missile behavior during tran-
sients when the missile is operating under controls utilizing these
methods of missile velocity stabilization, the dynamics of an idealized
missile-engine combination were investigated with the aid of a differ-
ential analyzer for a representative missile configuration. The drag
characteristics of the airframe (minus engine nacelles) considered are
shown in figure 12 as a plot of drag coefficient (based on wing area)
against flight Mach number for several angles of attack. Missile weight
was assumed to be 25,000 pounds, the ratio of engine combustion chamber
area to wing area was 0.0269, the wing loading was approximately 92 pounds
per square foot of projected wing area, and the cruise altitude was
60,000 feet. At cruise conditions the angle of attack was 3.5 degrees
and the drag curve in figure 11 is for this angle of attack.

    Velocity stabilization through angle of attack. - A block diagram
of a possible control system for cruise velocity stabilization utili-
zing aerodynamic forces is shown in figure 13. Missile flight Mach num-
ber is sensed and compared with the required Mach number in an error
detector. If any difference or error exists between measured and set
flight Mach numbers, this error signal acts through an angle of attack
control to vary the angle of attack in proportion to the magnitude of
the error. The control acts to increase angle of attack for overspeed
conditions and to decrease it for less than the required speed. As the
missile approaches the cruise velocity, the error decreases and the
angle of attack is restored to its equilibrium value. The engine con-
trol plays a relatively minor role in this system. Essentially, it
should be designed to maintain maximum safe thrust (i.e., critical thrust)
during underspeed conditions and a safe thrust (e.g., constant fuel flow
operation) when the missile is above the required speed. As such, this
can be a critical-point operation control of the type discussed pre-
viously with a fuel flow limiting device incorporated for overspeed con-
ditions. For the missile configuration studied, the time required to
change the attitude of the missile in pitch was assumed small compared
with the time required to change the flight speed, and the equations of
motion of the missile were solved with the dynamics of attitude changes
not considered. These dynamics must, of course, be considered in the
design of an actual control system.

The response of the missile considered to a disturbance in flight velocity under the action of the control system of figure 13 is shown in figure 14. Plotted are the variations of velocity and altitude with time for an initial departure from cruise velocity of minus 100 feet per second. The control considered was a simple proportional device with a gain of 3° angle of attack per 100 feet per second error in flight velocity. For this type of control action, the missile response is a damped oscillation in both velocity and altitude. The missile passes through the cruise velocity after about 1/2 minute but requires about 5 minutes before the oscillation damps to ±10 feet per second. During the initial oscillation, the flight altitude drops 4200 feet and after 5 minutes the oscillation has been damped to ±400 feet. Increasing the control gain, that is, increasing the change of angle of attack per unit error in flight speed, tends to decrease the response time and increase the damping; however, this is accompanied by an increased excursion in altitude during the first oscillation.

The control considered was a pure proportional control and is used merely to illustrate a principle of control rather than to represent optimum control design. A more elaborate system based on the same control principle using either derivative or integral as well as proportional action would probably decrease the oscillatory nature of the missile response and yield shorter response time as well. The response times involved are rather large, but are typical of aircraft velocity responses at high altitudes because such systems are characterized by high inertia and operate in a rarified atmosphere with attendant small restoring forces.

Velocity stabilization through engine thrust. - The second control system for stabilizing missile velocity during cruise requires supercritical engine operation. In order to investigate this type of stabilization, engine size was increased 19 percent so that the cruise point was as shown in figure 15. For this mode of engine operation the missile is essentially stable in velocity at cruise. For constant corrected fuel flow operation, the missile drag is greater than the thrust for overspeed conditions and a decelerating force exists which acts to restore the missile to cruise velocity; at flight velocities below cruise but above Mach number 2.8, thrust is greater than drag and an accelerating force exists which acts to restore the missile to cruise conditions. This restoring force is small, however, and the time required to return to equilibrium would be excessive. The response of the missile to a disturbance in flight velocity when the engine is operated at constant corrected fuel flow is shown in figure 16. Plotted are the variation with time of velocity and altitude for an initial disturbance in velocity of minus 100 feet per second. The angle of attack was assumed constant during the transient. The missile accelerates rather slowly and after about 7.25 minutes is within about 10 feet per second of the cruise velocity. Missile altitude varies during this time because of the change of lift with velocity and appears to approach a sustained oscillation, a limit cycle.

In order to decrease the time of response an engine thrust control
may be used to increase the magnitude of the restoring force. A block
diagram of such a system is shown in figure 17. The flight Mach num-
ber is measured and compared with the required value; if a difference
or error exists, this error signal acts through a fuel control to
increase thrust if the missile is below speed and to decrease thrust if
the missile is over speed, thus producing an increased restoring force
to bring the system to its equilibrium point. The use of high control
gain for such a system, that is, large changes of fuel flow per unit
error in velocity, can result in undesirable subcritical engine operation
during a transient. In order to prevent such a condition, a limiting
device may be incorporated in the control to prevent subcritical oper-
ation. Such a device could be the system considered earlier for attain-
ing critical operation by scheduling diffuser exit Mach number with
flight velocity. This system can be designed to act as a limiter rather
than as a primary control and will then limit effective fuel flow to
safe values during underspeed conditions. A minimum fuel flow limit
for overspeed conditions is also required to prevent combustion blow-
out.

The response of the missile acting under such a control scheme, that
is, thrust control with limiter action, is shown in figure 18 for an
initial displacement from cruise velocity of minus 100 feet per second
and with missile angle of attack held constant. The velocity returns to
the cruise value in a nearly linear manner with a slight superimposed
oscillation. About 3 minutes are required for the missile to attain
cruise velocity. Missile altitude oscillates during the transient
because of the change in lift with velocity and settles into a sustained
oscillation of small amplitude, about ±200 feet, with a period of
approximately 2 minutes. The response time of the particular system is
of the same order of magnitude as that of the aerodynamic control system,
but it must be remembered that the engine size is 19 percent greater
than that considered previously and that maximum available restoring
force was attained with the limiting control. The response time deter-
mined may therefore be considered to represent a minimum for this sys-
tem. For smaller increases in engine size, the available restoring
force decreases and larger response times result.

One relatively simple method for automatically obtaining a high gain
control for cruise velocity stabilization is suggested in reference 6.
This system operates by controlling the fuel flow to maintain a constant
diffuser pressure ratio P_2/p_0. The operating map of the engine under
such control action is shown in figure 19, where corrected propulsive
thrust is plotted against flight Mach number at several constant diffuser
pressure ratios. The system has a high degree of inherent stability and
essentially needs no flight Mach number setting device, since setting a
value of P_2/p_0 sets the cruise flight Mach number; however, the accu-
rate calibration of the engine required may be difficult to attain.

The engine must be operated supercritically during cruise under this control scheme, and thus will be oversized, as for the thrust control system previously discussed. In addition, provision must be made to prevent subcritical engine operation since, as indicated in figure 19, engine thrust is not defined at constant diffuser pressure ratio in this region. Missile response under such a control scheme would be very similar to that shown in figure 18.

The choice of a cruise-velocity control system depends upon many factors. Among these are the requirements of the flight plan, the requirements of the guidance or navigation system, and the nature of disturbances which may be encountered along a flight path. If it is necessary that missile weight be kept at a minimum in order to achieve a specified range, then critical engine operation and use of aerodynamic control for velocity stabilization are indicated. If missile weight is not critical, thrust control with supercritical engine operation during cruise offers the advantages of inherent stability and a minimum of variation in altitude. The missile guidance system may require a fast velocity response so that the missile may stay within the limits of a time-programmed flight plan. In this event, aerodynamic stabilization with high control gain appears to offer the best solution. The nature of the disturbances expected during flight plays an important role in the selection of the velocity control system. If the disturbances are slow acting and of small magnitude, either control scheme would be satisfactory. On the other hand, impulse-like disturbances of large repetition rate might cause serious reduction of range for either control scheme because of sensitivity to flight Mach number, and the loss of range during transients is an important consideration in the selection of a control system.

The selection of a cruise velocity control system must therefore be an engineering compromise based upon an evaluation of the requirements of the particular missile configuration and flight plan and the nature of the disturbances expected during the flight.

CONCLUSIONS

An analysis based on the calculated performance of a fixed-geometry ram jet of a configuration suitable for strategic supersonic missile propulsion was used to evaluate control requirements and parameters. The following conclusions were made:

1. For engine operation at minimum specific fuel consumption, the ram jet should be operated with critical diffuser conditions. Such operation may be attained by several control systems:

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APPENDIX - SYMBOLS

A area, sq ft

C_D missile drag coefficient based on wing area

F_p propulsive thrust, lb

M Mach number

P total pressure, lb/sq ft

p static pressure, lb/sq ft

T total temperature, $^\circ$R

W_f fuel flow, lb/hr

α angle of attack, deg

η_b combustion efficiency

τ engine total temperature ratio, T_4/T_2

Subscripts:

R required value of a controlled variable

0 free stream

1 diffuser entrance

2 diffuser exit

3 downstream of flame holders

4 nozzle entrance

5 nozzle throat

6 nozzle exit

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Diffuser

Combustion chamber

Nozzle

Station 0

1

2

3

4

5

6

NACA
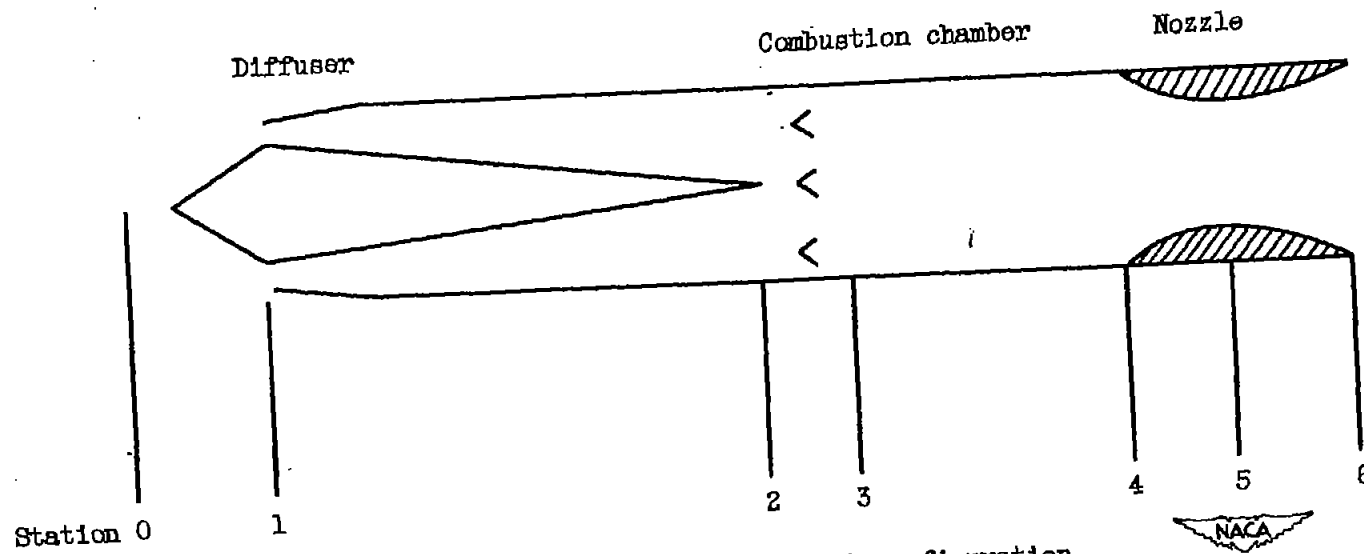
Figure 1. - Schematic drawing of ram-jet configuration.
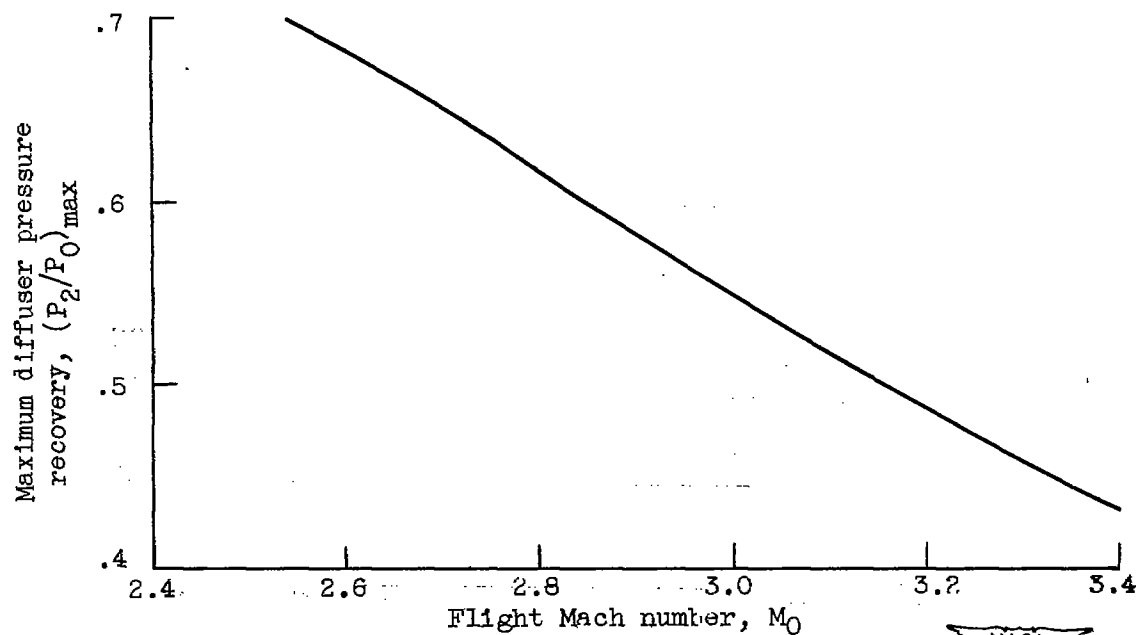
Figure 2. - Diffuser pressure recovery characteristic assumed for calculations. Fixed diffuser geometry designed for flight Mach number of 3.0.

Flight Mach number
M_0

3.4
3.3
3.2
3.1
3.0
2.9
2.8
2.7
2.6

Corrected propulsive thrust, F_p/A_2p_0

NACA

Corrected effective fuel flow, $\eta_p W_f/A_2 p_0$
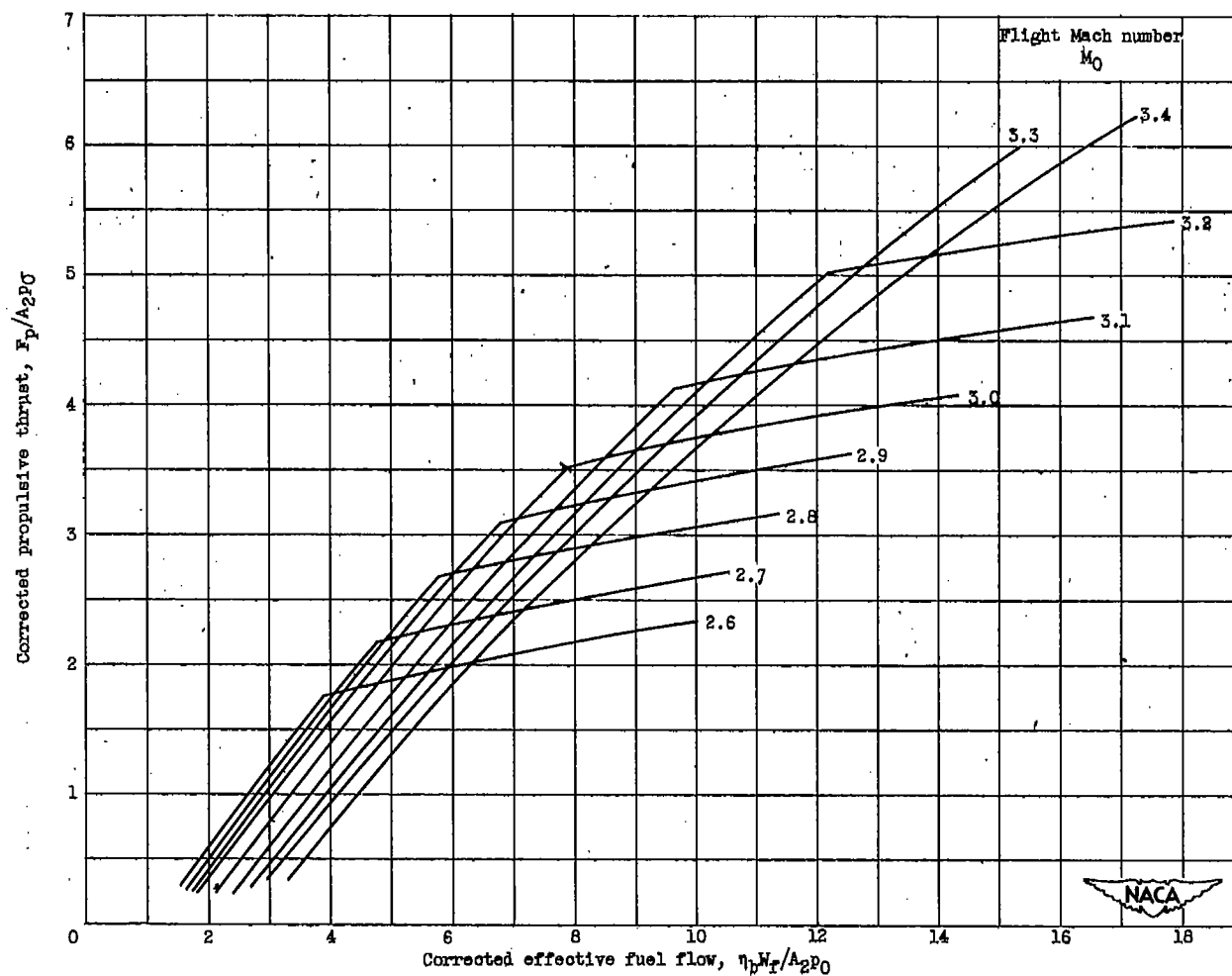
(a) Variation of thrust with effective fuel flow.

Figure 3. - Performance of ram-jet engine.
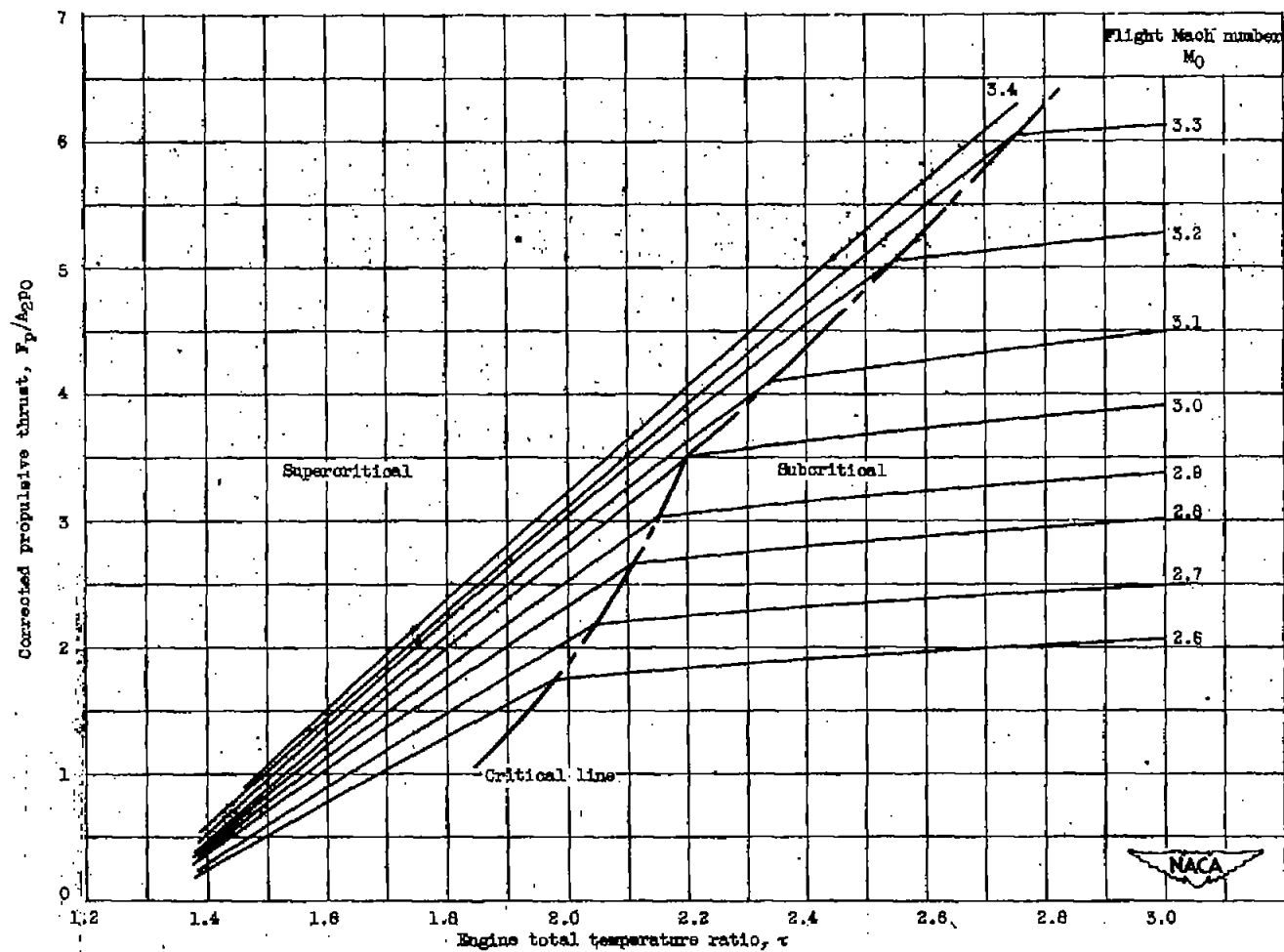
(b) Variation of thrust with engine temperature ratio.

Figure 3. - Continued. Performance of ram-jet engine.
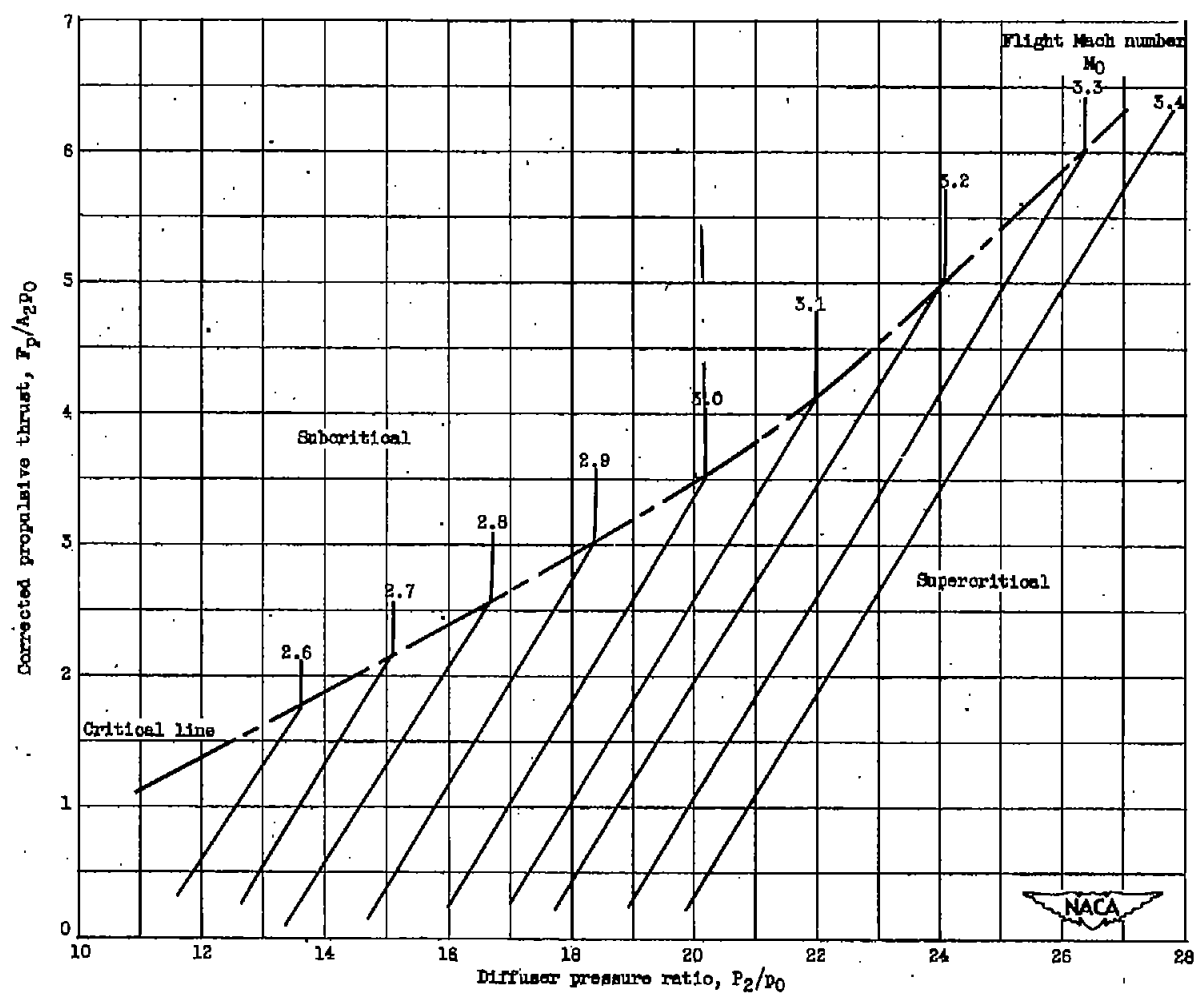
(c) Variation of thrust with diffuser pressure ratio.

Figure 3. - Continued. Performance of ram-jet engine.
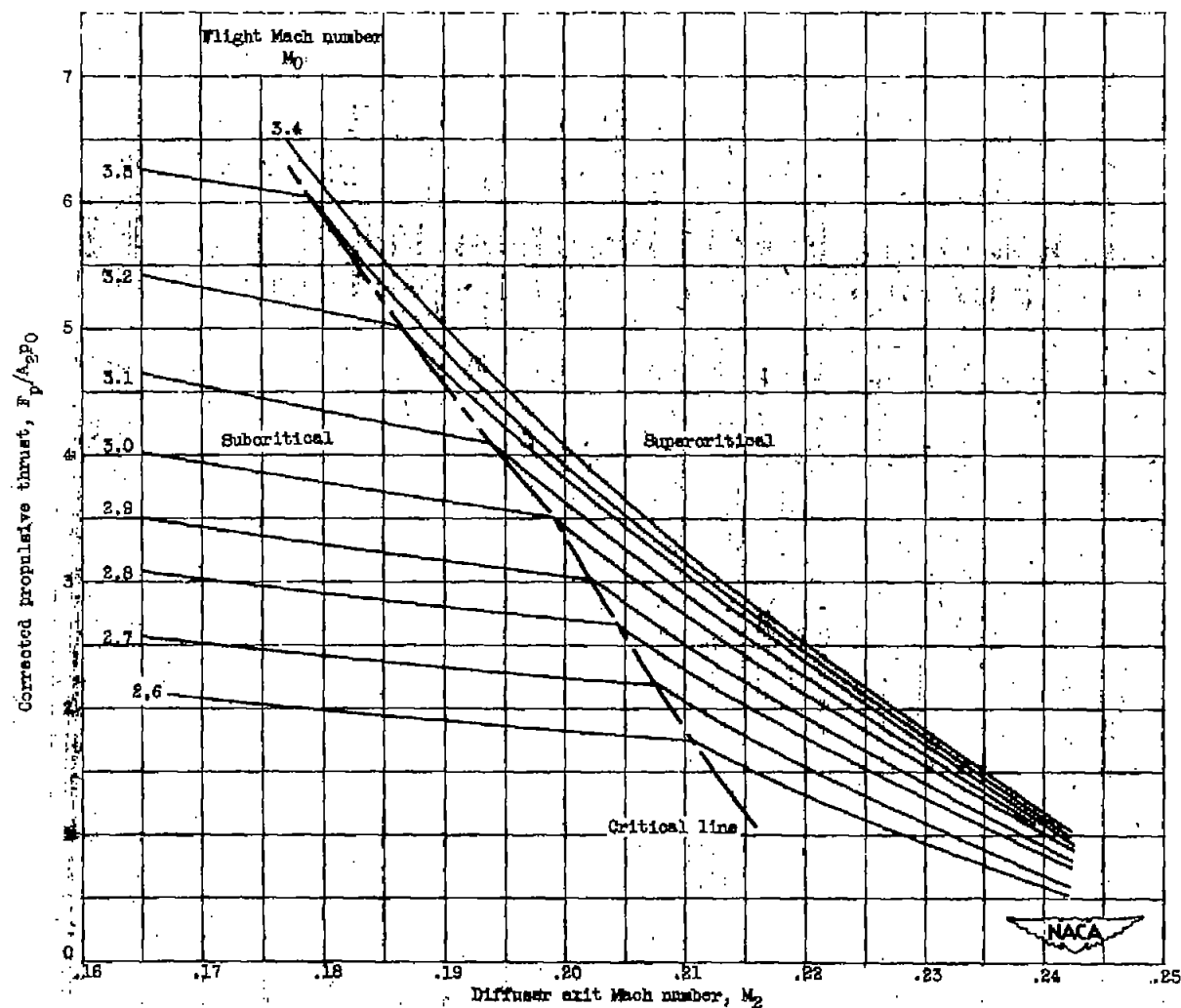
(a) Variation of thrust with diffuser exit Mach number.

Figure 3. - Concluded. Performance of ram-jet engine.
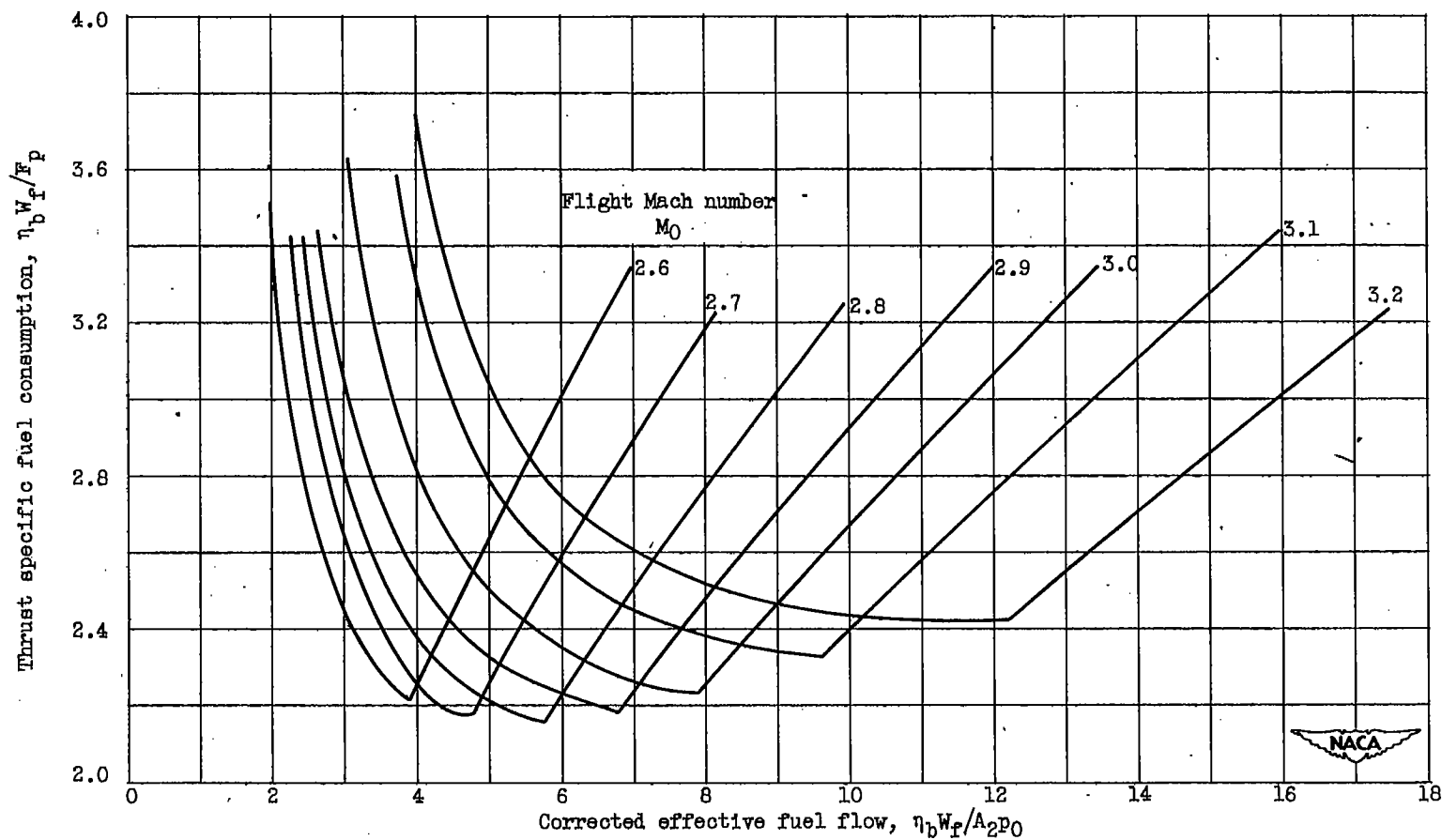
(a) Variation of thrust specific fuel consumption with effective fuel flow.

Figure 4. - Economy of ram-jet engine operation.
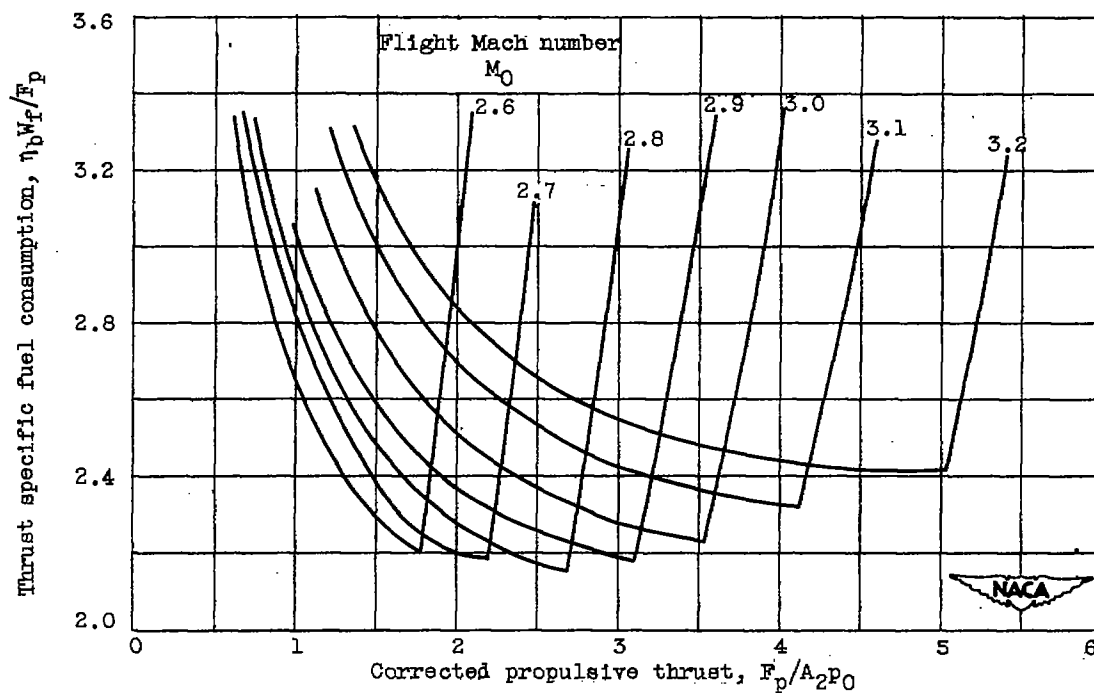
(b) Variation of thrust specific fuel consumption with propulsive thrust.

Figure 4. - Concluded. Economy of ram-jet engine operation.

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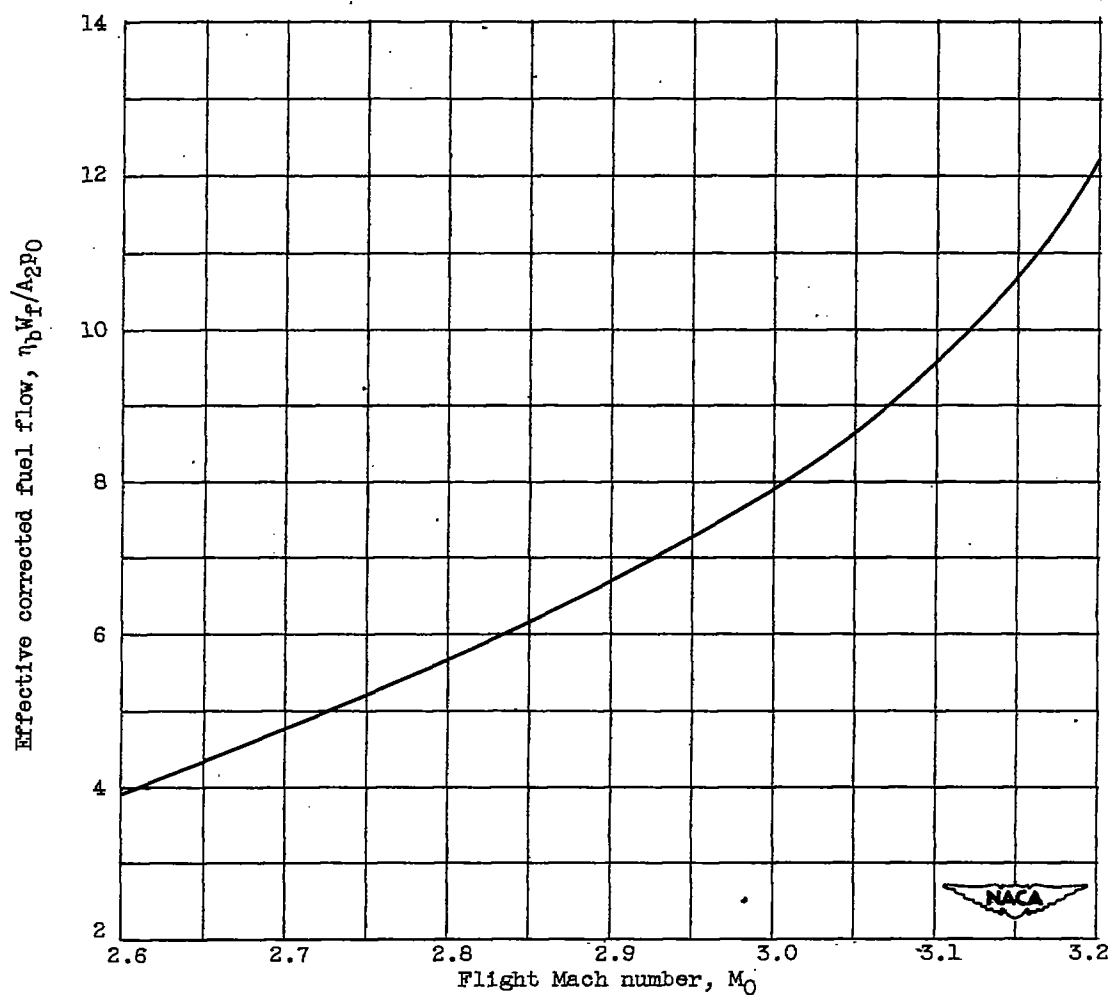
Figure 5. - Required effective fuel flow for critical engine operation as function of flight Mach number.
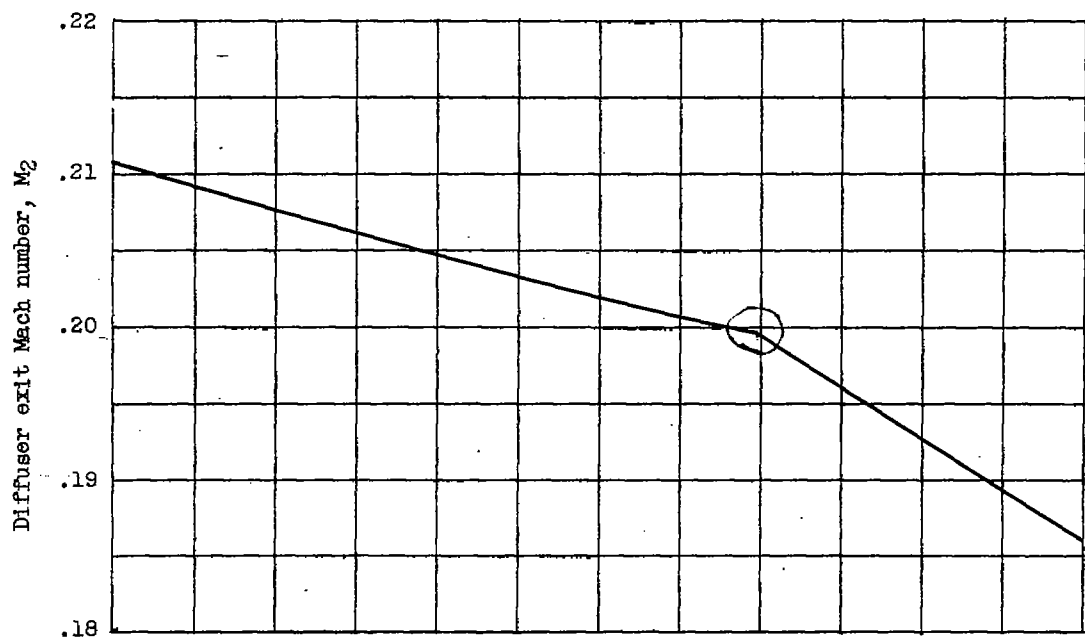
(a) Diffuser exit Mach number.
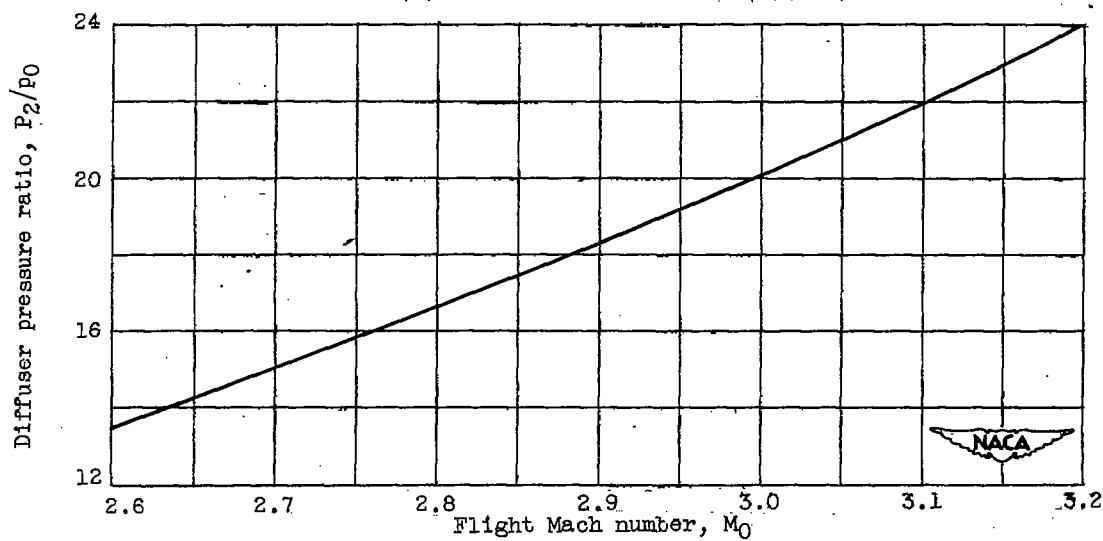
(b) Diffuser pressure ratio.

Figure 6. - Required variation of engine variables with flight Mach number
for critical engine operation.

M_0 (measured) → Scheduler → $(P_2/P_0)_R$ → ⊖ → Error → Fuel control → W_f → Engine → P_2/P_0 →

P_2/P_0 (measured)
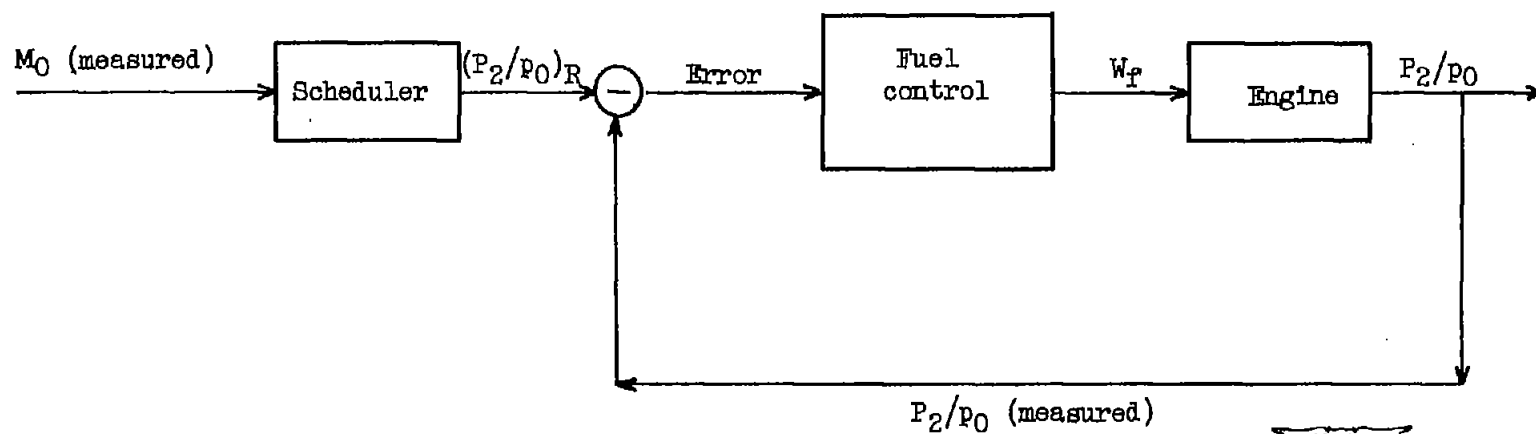
Figure 7. - Block diagram of control system for maintaining critical engine operation by controlling diffuser pressure ratio.
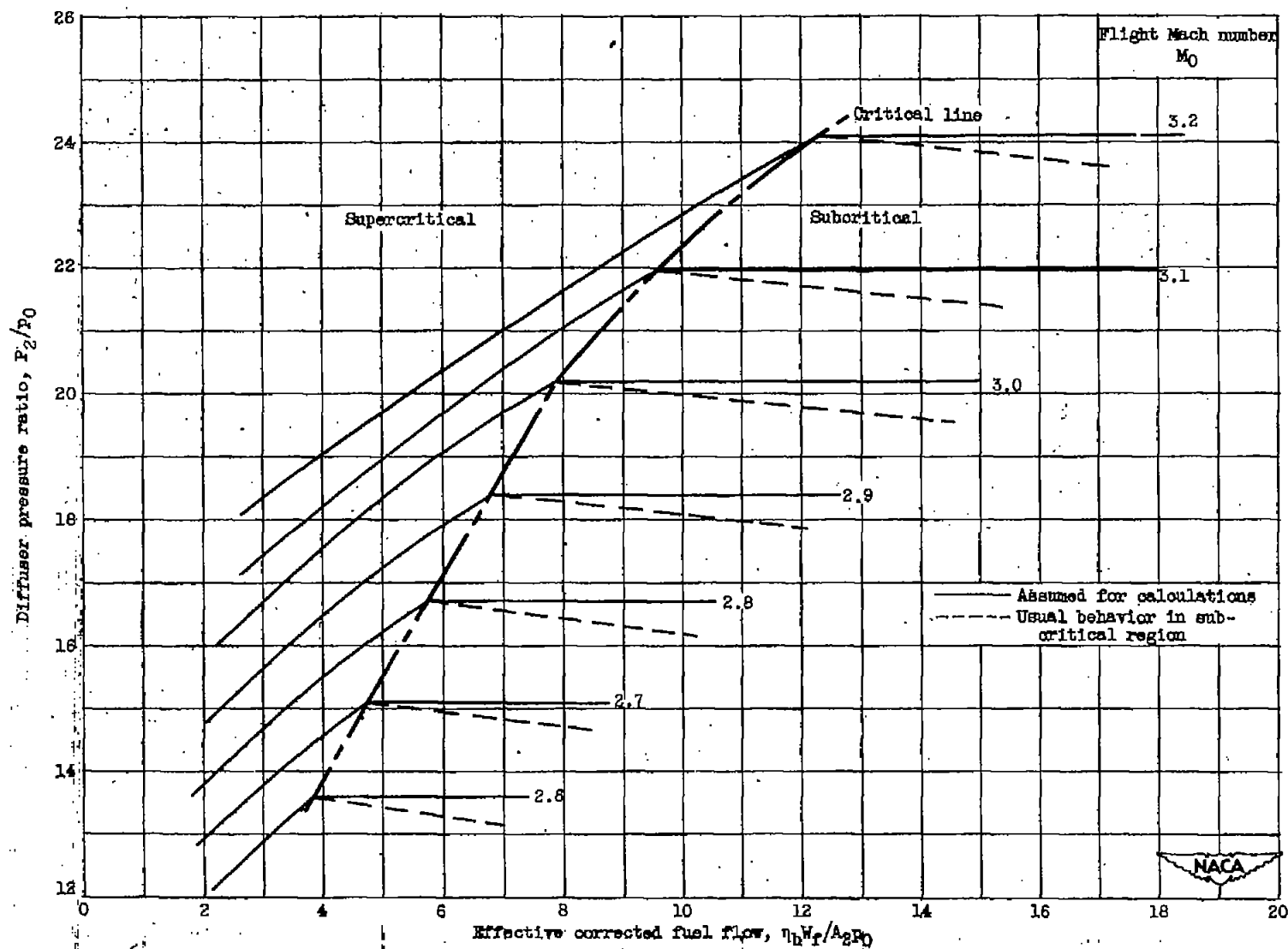
Figure 8. - Variation of diffuser pressure ratio with effective fuel flow at several constant flight Mach numbers.
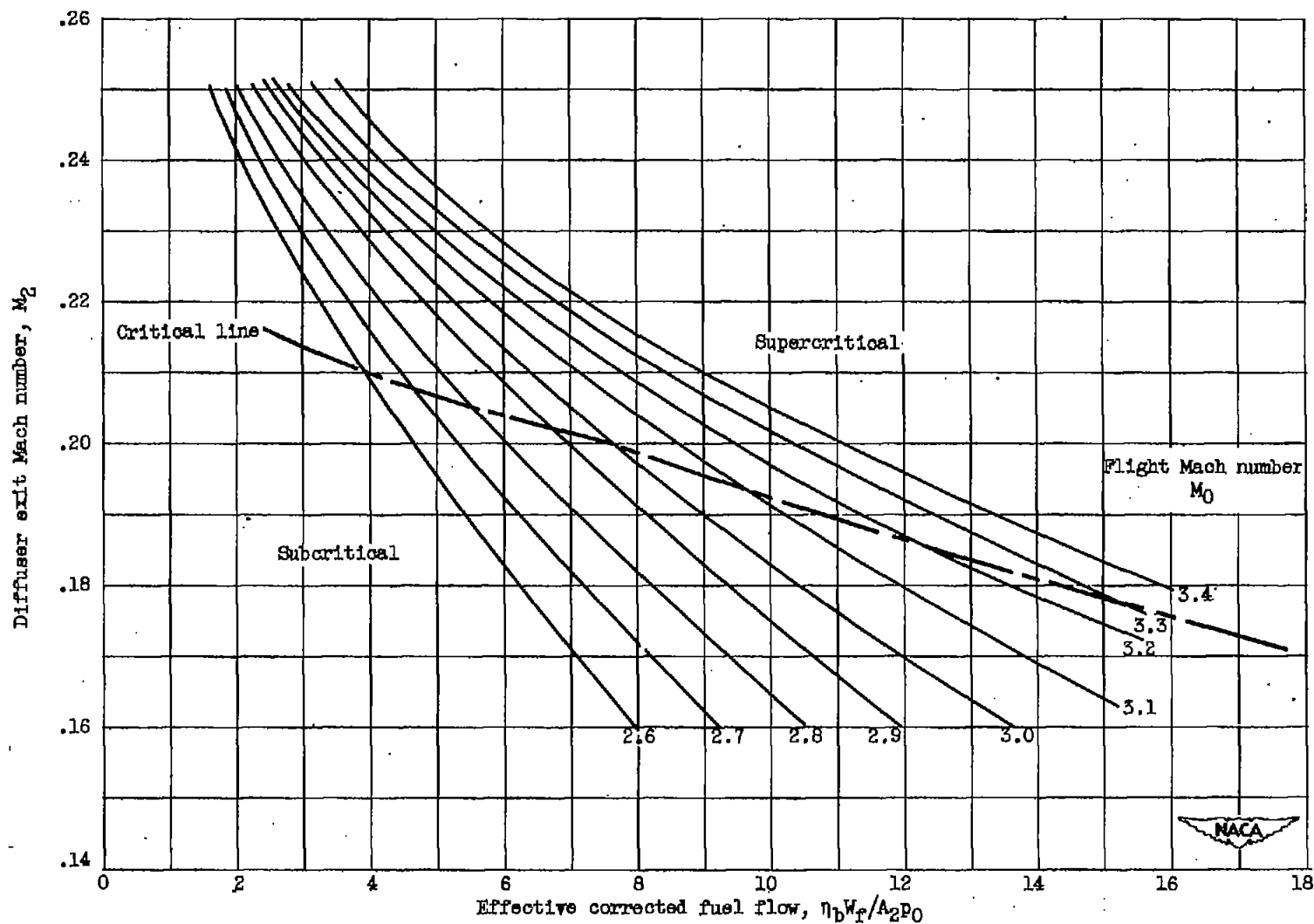
Figure 9. - Variation of diffuser exit Mach number with effective fuel flow at several constant flight Mach numbers.
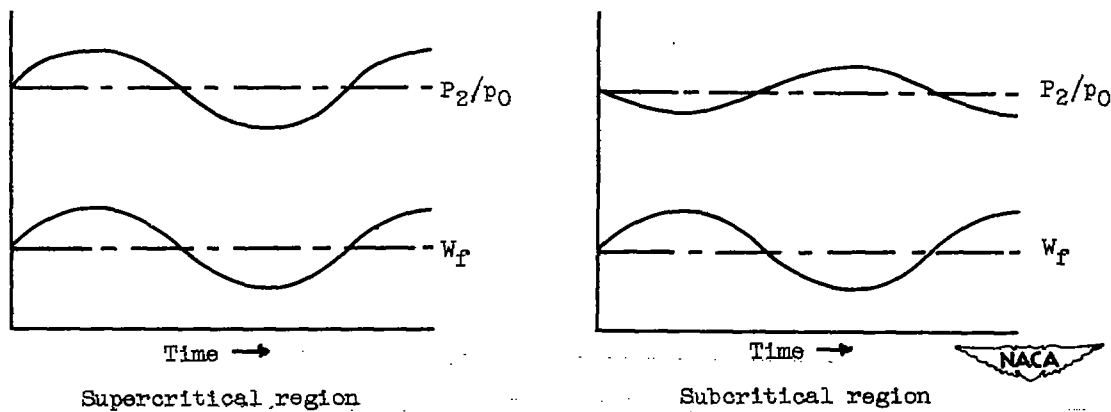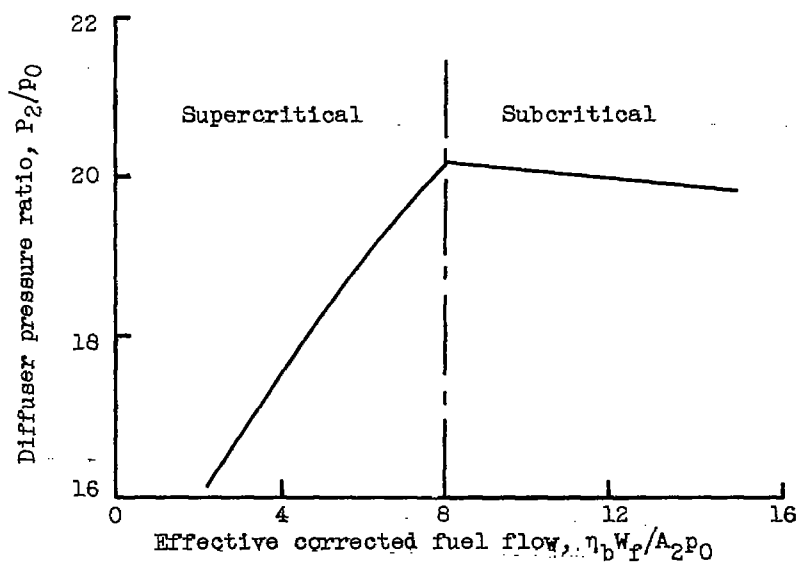
Figure 10. - Principle of operation of optimizing control system.
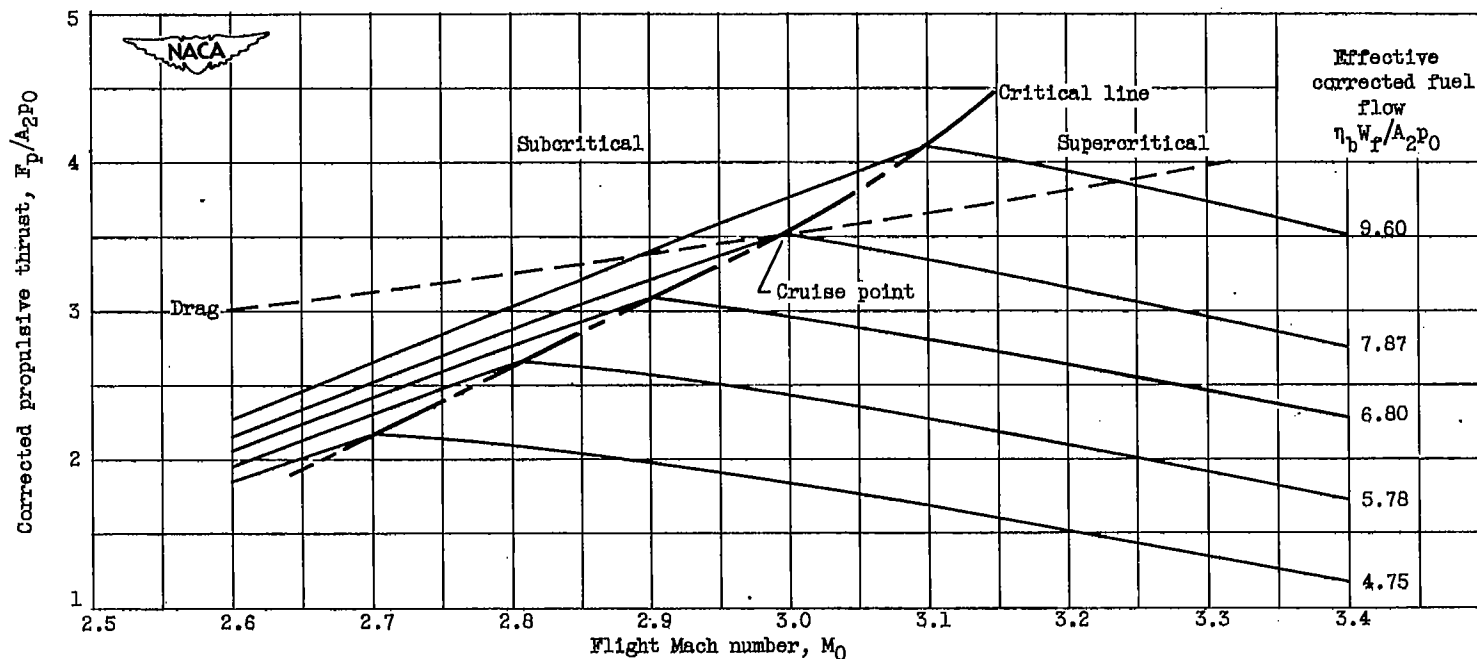
(a) Thrust as a function of Mach number for several constant effective corrected fuel flows.

Figure 11. - Ram-jet and missile performance for critical engine operation at cruise point.
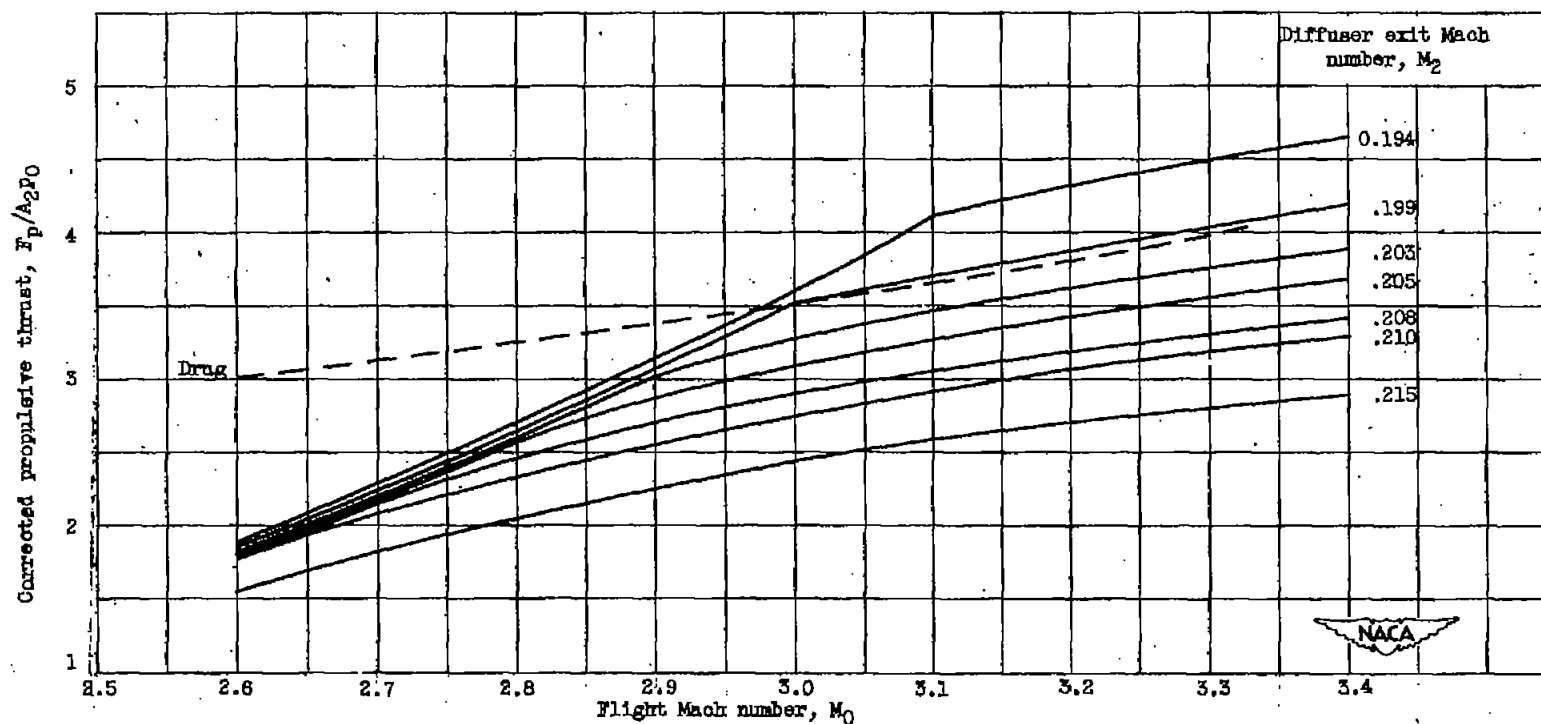
(b) Thrust as a function of Mach number for several constant diffuser exit Mach numbers.

Figure 11. - Concluded. Ram-jet and missile performance for critical engine operation at cruise point.
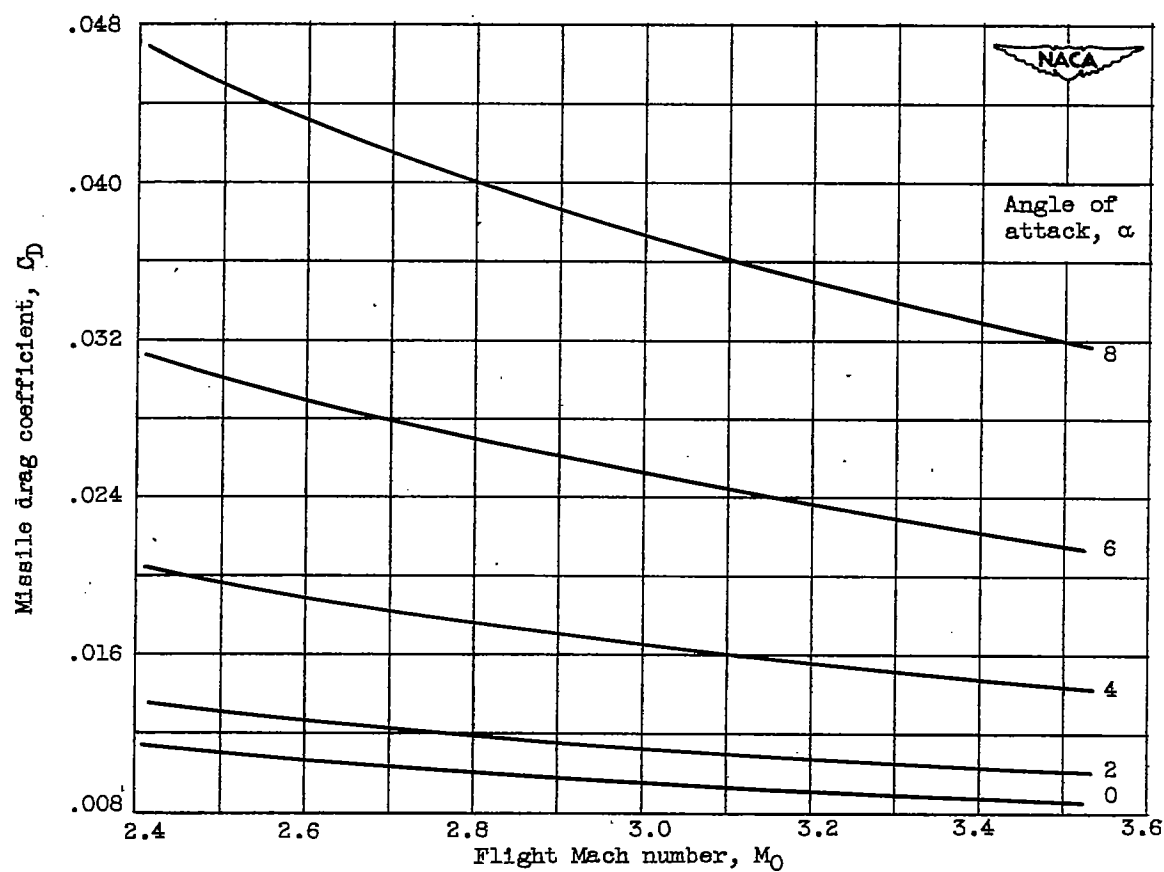
Figure 12. - Drag characteristics of missile. Missile weight, 25,000 pounds; ratio of engine combustion chamber area to wing area, 0.0269; wing loading, 92 pounds per square foot; cruise altitude, 60,000 feet.
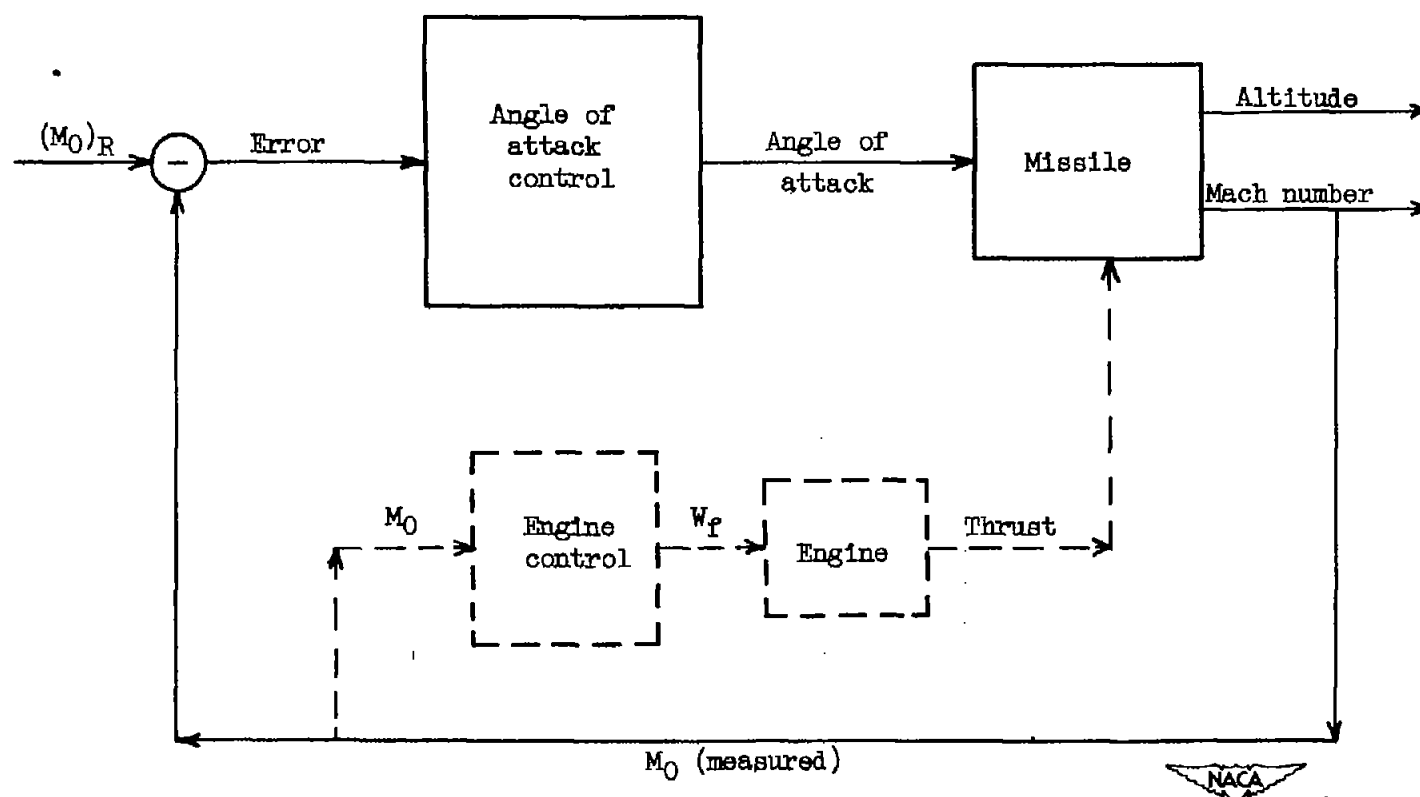
Figure 13. - Block diagram of control system for stabilization of flight velocity through angle of attack.
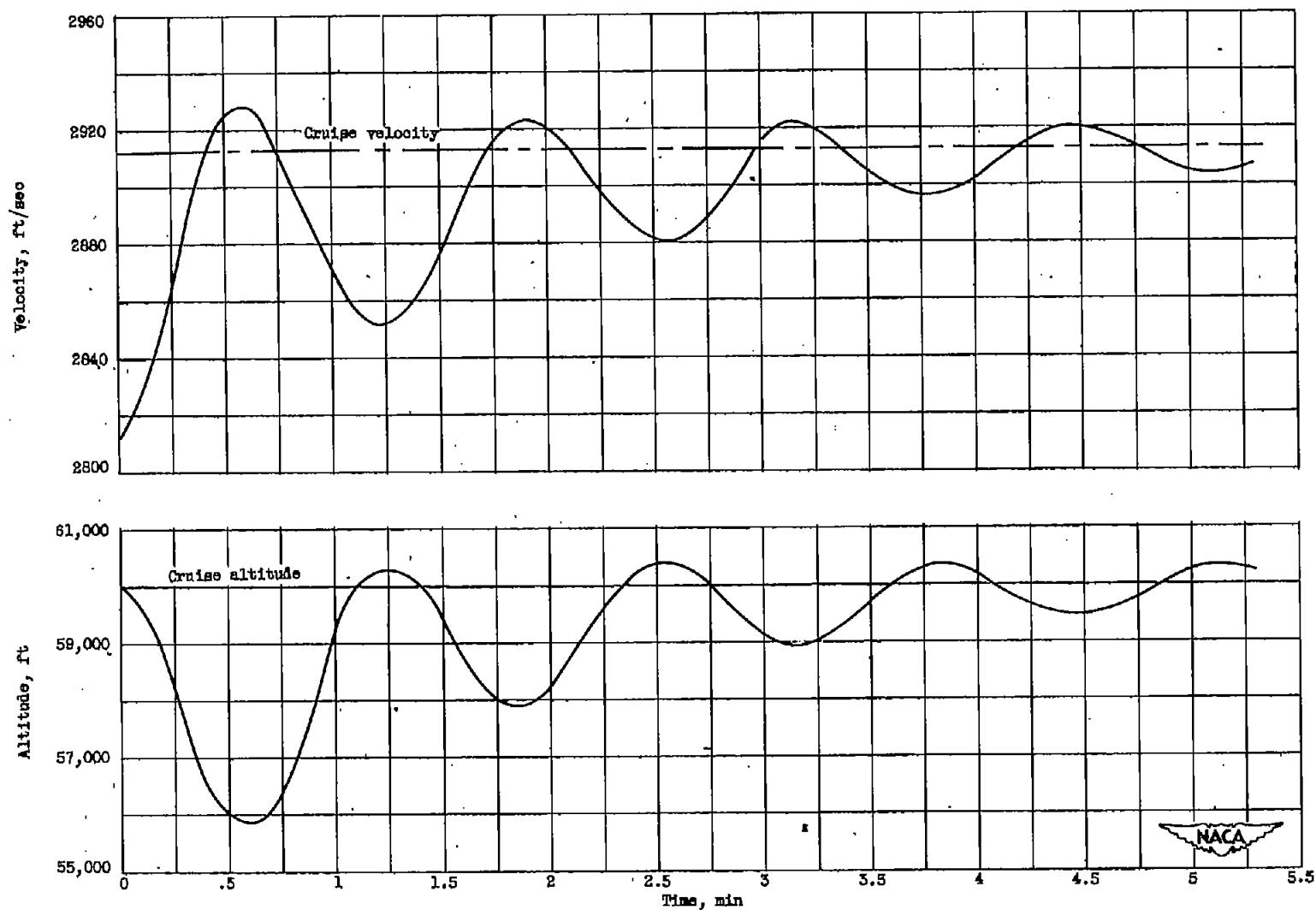
Figure 14. - Response of missile to velocity disturbance with aerodynamic velocity stabilization and critical engine operation.
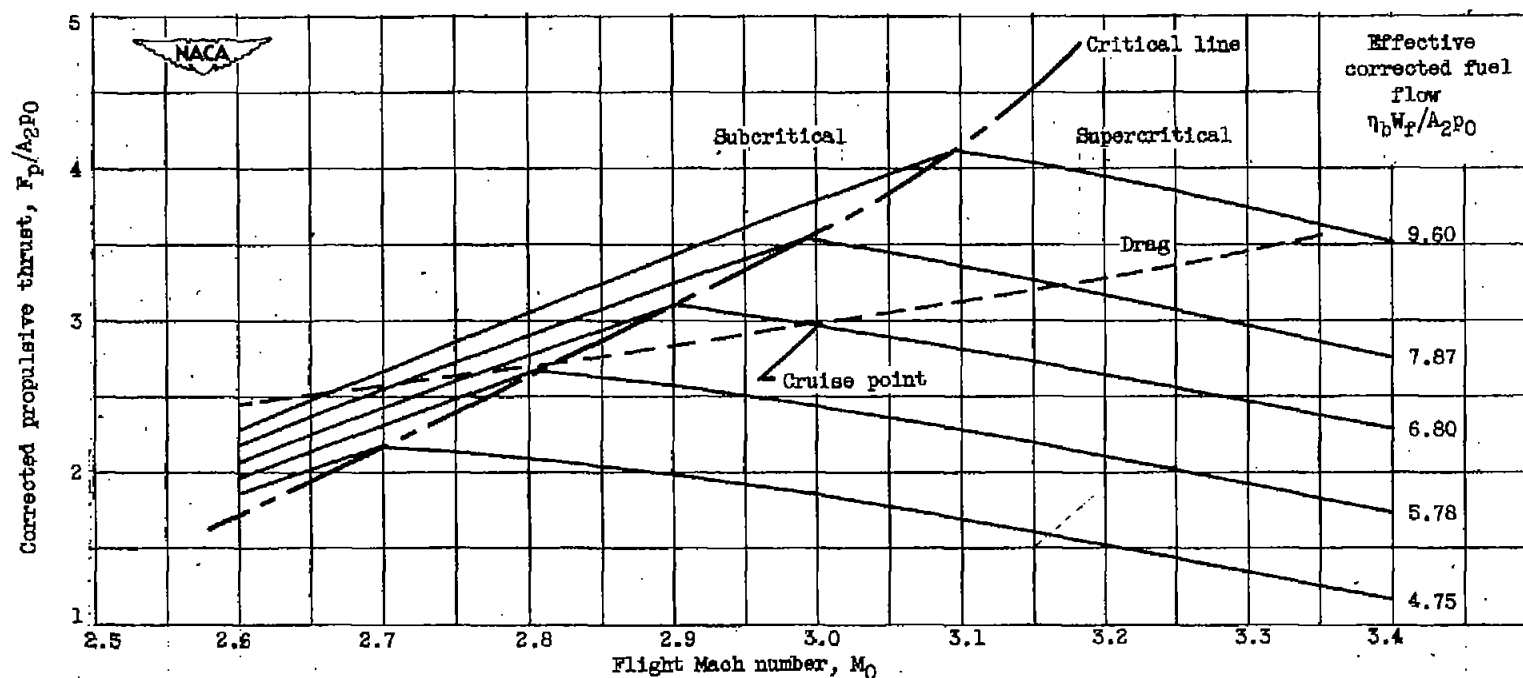
Figure 15. - Ram-jet and missile performance with supercritical engine operation at cruise point.
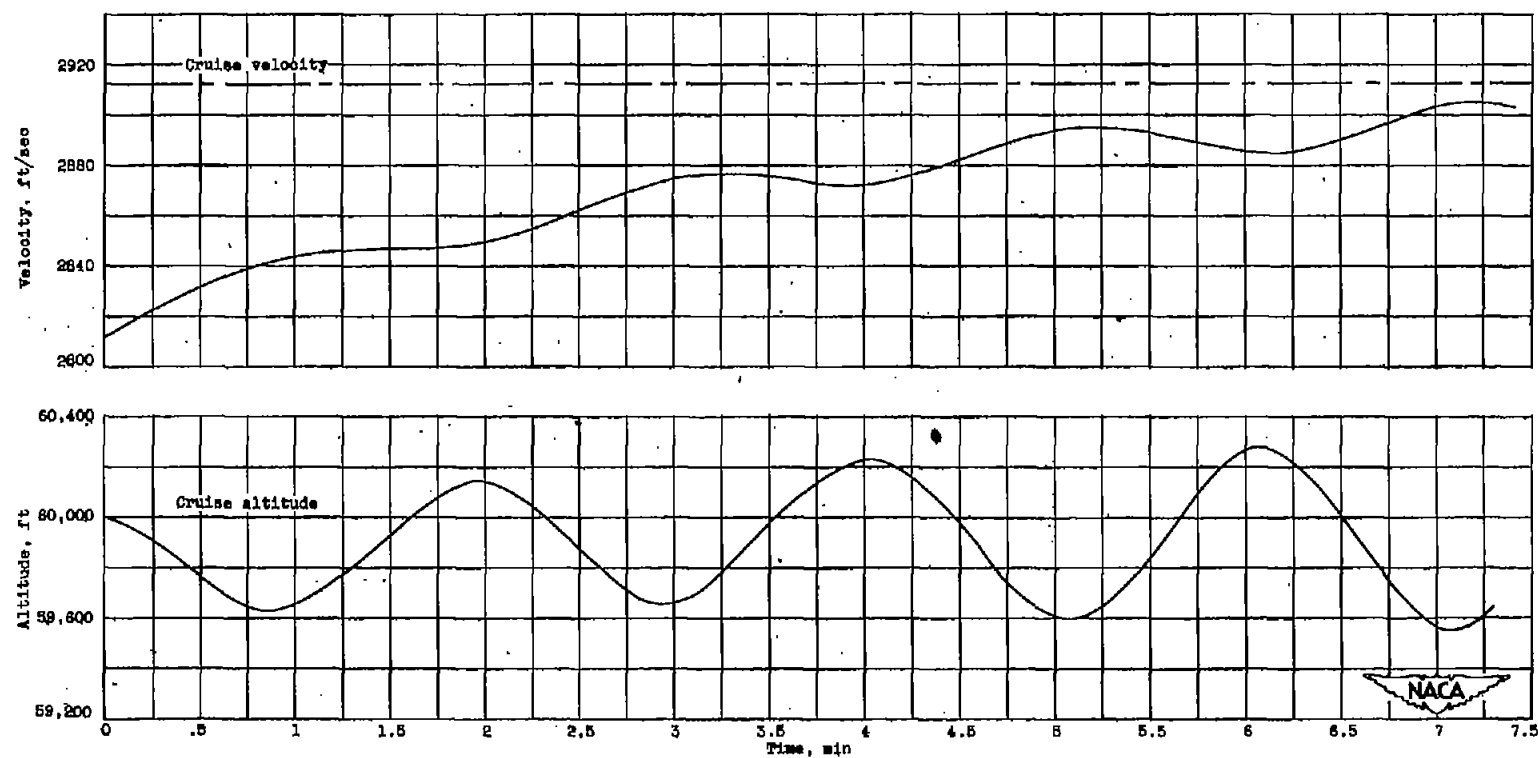
Figure 16. - Response of missile to velocity disturbance with engine operating at constant corrected fuel flow. Missile at constant angle of attack.
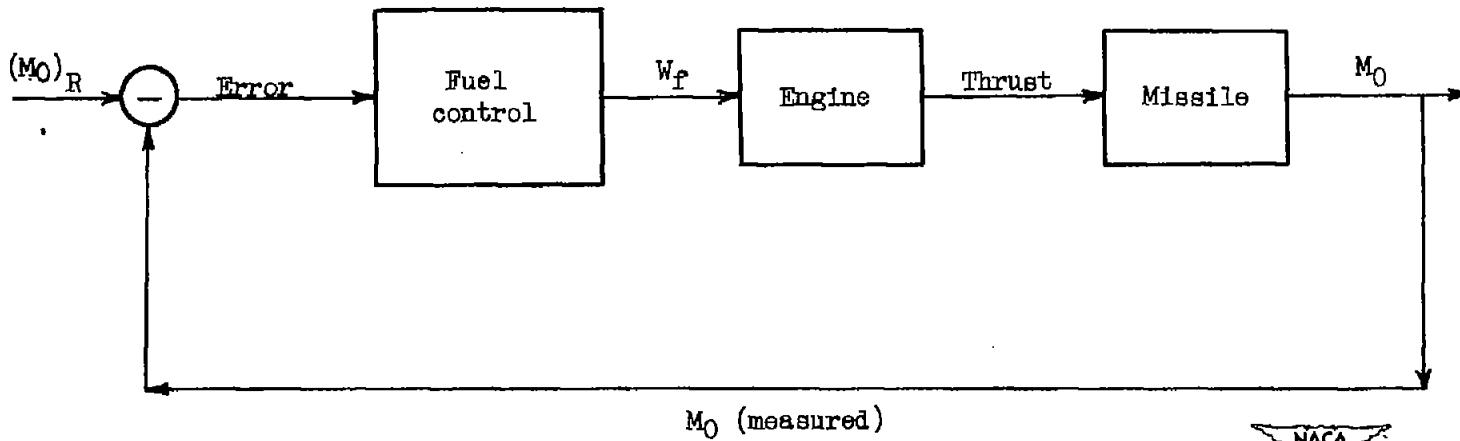
Figure 17. - Block diagram of control system for stabilization of flight Mach number through engine thrust with supercritical engine operation at cruise point.
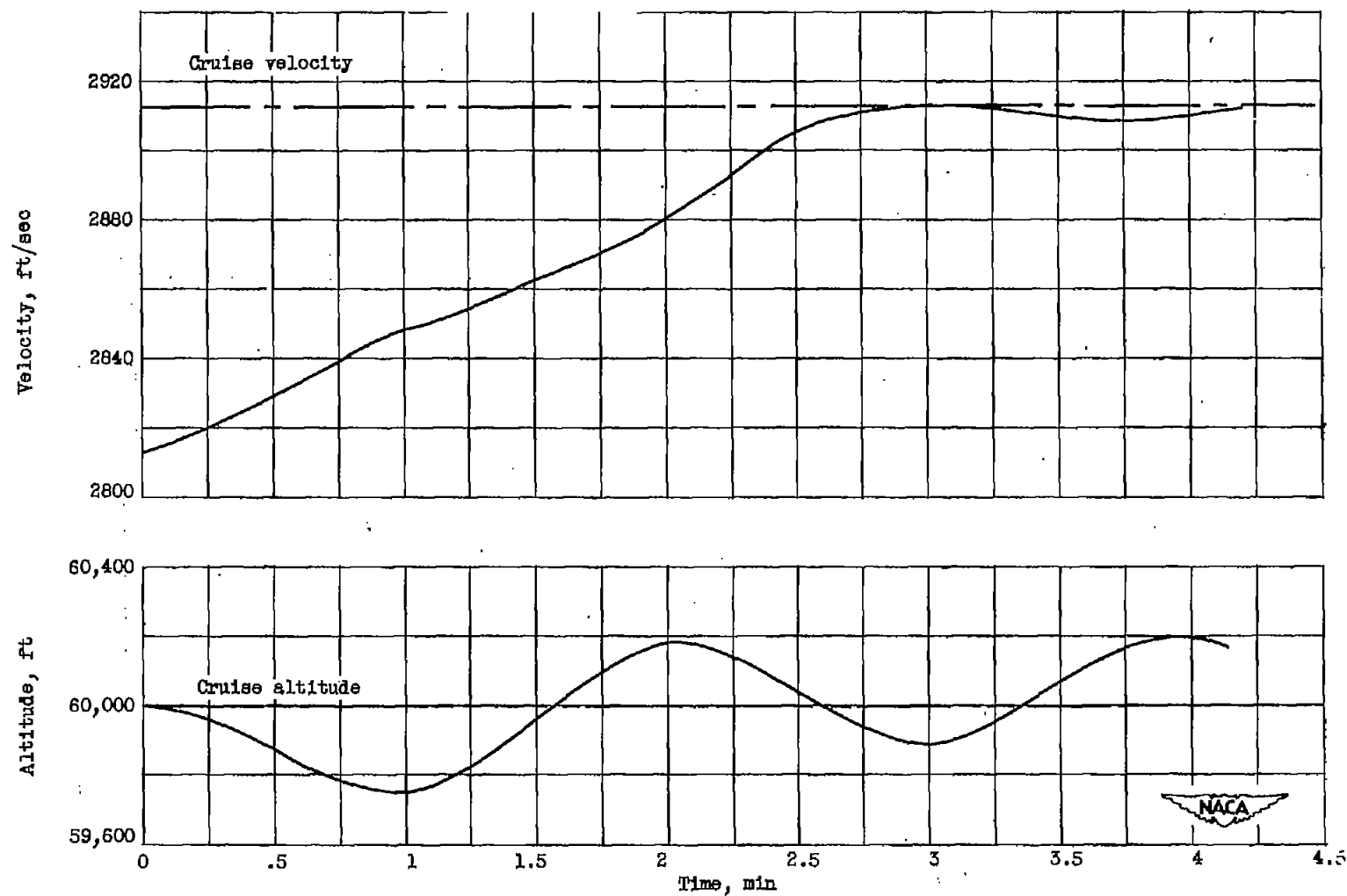
Figure 18. - Response of missile to velocity disturbance with engine thrust cruise velocity control. Missile at constant angle of attack.
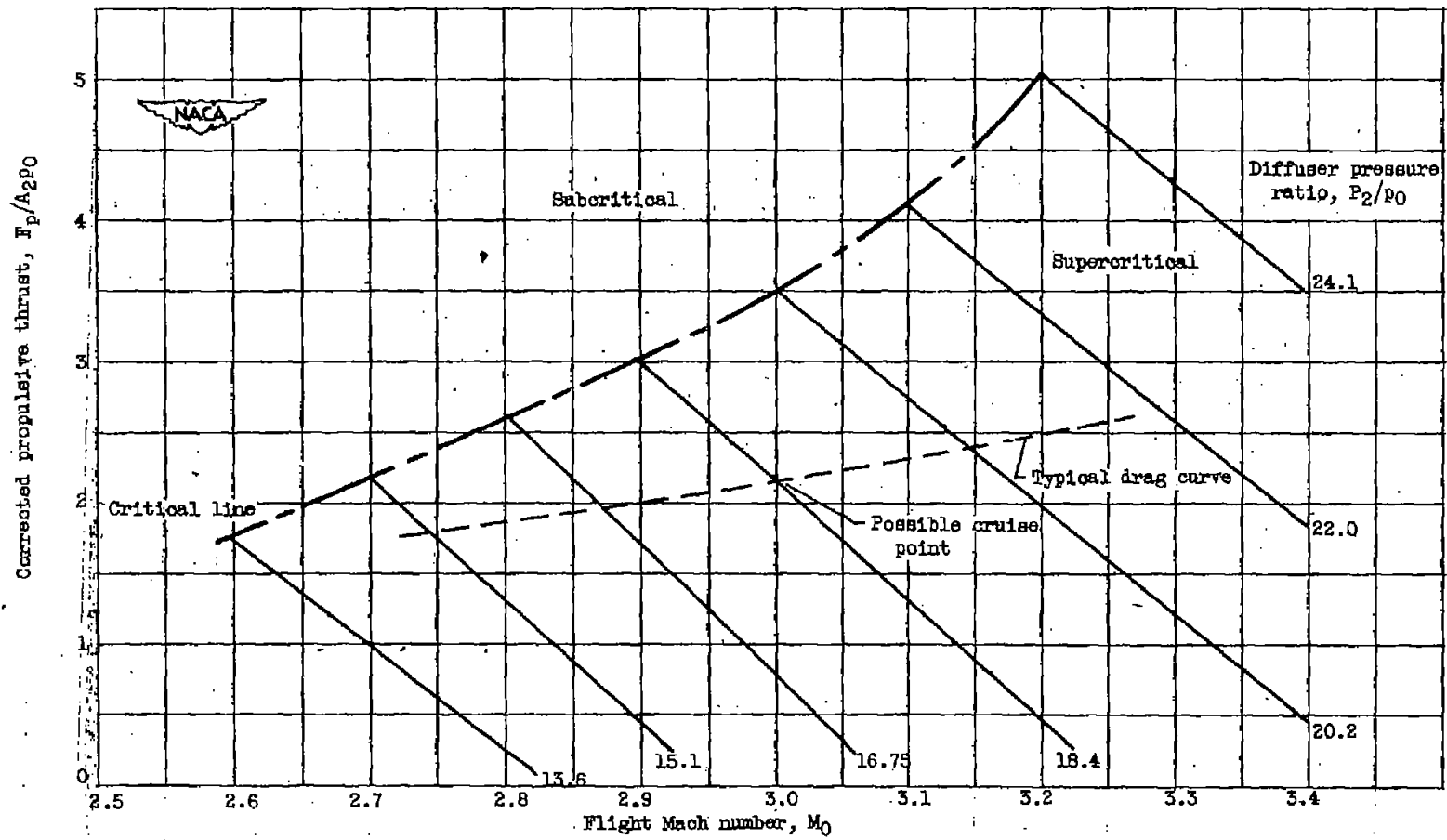
Figure 19. - Performance of ram-jet engine with thrust as function of flight Mach number at constant diffuser pressure ratios.